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International Journal of Hydrogen Energy 888 (1888) 888-888



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The grand unified theory of classical quantum mechanics

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Abstract

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A theory of classical quantum mechanics (CQM) is derived from first principles that successfully applied physical laws on all scales. Using Maxwell's equations, the classical wave equation is solved with the constraint that a bound electron cannot radiate energy. By further application of Maxwell's equations to electromagnetic and gravational fields at particle production, the Schwarzschild metric (SM) is derived from the classical wave equation which mattines general relativity to include conservation of spacetime in addition to momentum and matter/energy. The result gives a fait all relationship between Maxwell's equations, special relativity, and general relativity. It gives gravitation from the along to the cosmos. © 2001 Published by Elsevier Science Ltd on behalf of the International Association for Hydrogram energy.

1. Introduction

A theory of classical quantum mechanics (CQM), derived from first principles, successfully applies physical laws on... all scales [1]. The classical wave equation is solved with the constraint that a bound electron cannot radiate energy. The mathematical formulation for zero radiation band, Maxwell's equations follows from a derivation [2]. The function that describes the motion of the must not possess spacetime Fourier compo synchronous with waves traveling at in the hading the CQM gives closed form solutions for the stability of the n=1 state and the of the excited p and states, the equation of the pho lectron in excited and photon which states, the equation of the predict the wave particle quality behavior of particles and light. The current and charge descrity functions of the electron may be directly posterily interpreted. For example, spin angular month that wills from the motion of negatively charged in a suring systematically, and the equation for angular momentum, r x p, can be applied directly to the wave function (a chirrent density function) that describes the electron. The magnetic moment of a Bohr magneton, Stern

For any kind of wave advancing with limiting velocity and capable of transmitting signals, the equation of front propagation is the same as the equation for the front of a light wave. By applying this condition to electromagnetic and gravitational fields at particle production, the Schwarzschild metric (SM) is derived from the classical wave equation which modifies general relativity to include conservation of spacetime in addition to momentum and matter/energy. The result gives a natural relationship between Maxwell's equations, special relativity, and general relativity. It gives gravitation from the atom to the cosmos. The universe is time harmonically oscillatory in matter energy and spacetime expansion and contraction with a minimum radius that is the gravitational radius. In closed form equations with fundamental constants only, CQM gives the deflection of light by stars, the precession of the perihelion of Mercury, the particle masses, the Hubble constant, the age of the universe, the observed acceleration of the expansion, the power of the

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Gerlain exteriment, g factor, Lamb shift, resonant line width and single spection rules, correspondence principle, wave practice deality, excited states, reduced mass, rotational energies, and momenta, orbital and spin splitting, spin-orbital coupling, Knight shift, and spin-nuclear coupling, inhization energies of two electron atoms, elastic electron scattering from helium atoms, and the nature of the chemical bond are derived in closed form equations based on Maxwell's equations. The calculations agree with experimental observations.

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universe, the power spectrum of the universe, the microwave background temperature, the uniformity of the microwave
 background radiation at 2.7 K with the microkelvin spatial variation observed by the DASI, the observed violation of the GZK cutoff, the mass density, the large-scale structure of the universe, and the identity of dark matter which matches the criteria for the structure of galaxies. In a special case wherein the gravitational potential energy density of a blackhole equals that of the Plank mass, matter converts to energy and spacetime expands with the release of a gamma
 ray burst. The singularity in the SM is eliminated.

2. Classical quantum theory of the atom based on Maxwell's equations

One-electron atoms include the hydrogen atom, He⁺,

15 Li²⁺, Be³⁺, and so on. The mass-energy and angular
momentum of the electron are constant, this requires that

17 the equation of motion of the electron be temporally and
spatially harmonic. Thus, the classical wave equation

19 applies and

$$\left[\nabla^2 - \frac{1}{v^2} \frac{\partial^2}{\partial t^2}\right] \rho(r, \theta, \phi, t) = 0, \tag{1}$$

where $\rho(r, \theta, \phi, t)$ is the time-dependent charge-density function of the electron in time and space. In general, the wave equation has an infinite number of solutions. To arrive at the solution which represents the electron, a suitable boundary condition must be imposed. It is well known from experiments that each single atomic electron of a given isotope radiates to the same stable state. Thus, the phys boundary condition of nonradiation of the bound was imposed on the solution of the wave equation time-dependent charge-density function of the The condition for radiation by a moving point 31 by Haus [2] is that its spacetime Fou possess components that are synchronic eling at the speed of light. Conve ble of moving the condition for nonradiation point charges that comprises a nsity function is 35

For nonradiative state, the therent-density function must NOT possess states were ourier components that are synchronous must be speed of light.

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The time; sadial, and angular solutions of the wave equation are separable. The motion is time harmonic with frequency ω_n. A constant angular function is a solution to the
wave equation. The solution for the radial function which
satisfies the boundary condition is a radial delta function

$$f(r) = \frac{1}{r^2} \delta(r - r_0)$$
 (2)

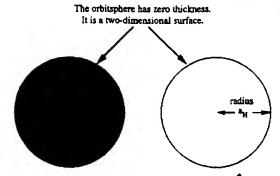


Fig. 1. The orbitsphere is a two-dimensional spherical shell with the Bohr radius of the hydrogen atom.

which defines a constant charge function of a spherical shell where $r_n = nr_1$. Given time harmonic fit too, and a radial delta function, the relationship between a allowed radius and the electron wavelength.

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$$2\pi r_n = \lambda_n. \tag{3}$$

Using the de Broglie that ship for the electron mass where the coordinates are spherous,

$$\lambda_n = \frac{h}{p_{\text{max}}} = \frac{1}{h_{\text{max}}} \tag{4}$$

and the magnitude of the velocity for every point on the

$$v_n = \frac{1}{16\pi^2}.$$
 (5)

The sum of the L_i, the magnitude of the angular momentum of each infinitesimal point of the orbitsphere of mass m_i , must be constant. The constant is \hbar .

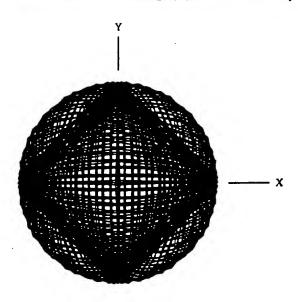
$$\sum |\mathbf{L}_i| = \sum |\mathbf{r} \times m_i \mathbf{v}| = m_e r_n \frac{\hbar}{m_e r_e} = \hbar. \tag{6}$$

Thus, an electron is a spinning, two-dimensional spherical surface, called an electron orbitsphere, that can exist in a bound state at only specified distances from the nucleus as shown in Fig. 1. The corresponding current function shown in Fig. 2 which gives rise to the phenomenon of spin is derived in the "Spin Function" section.

Nonconstant functions are also solutions for the angular functions. To be a harmonic solution of the wave equation in spherical coordinates, these angular functions must be spherical harmonic functions. A zero of the spacetime Fourier transform of the product function of two spherical harmonic angular functions, a time harmonic function, and an unknown radial function is sought. The solution for the radial function which satisfies the boundary condition is also a delta function given by Eq. (2). Thus, bound electrons are described by a charge-density (mass-density) function which is the product of a radial delta function, two angular

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VIEW ALONG THE Z AXIS

Fig. 2. The current pattern of the orbitsphere from the perspective of looking along the z-axis. The current and charge density are confined to two dimensions at $r_n = nr_1$. The corresponding charge density function is uniform.

1 functions (spherical harmonic functions), and a time harmonic function.

$$\rho(r,\theta,\phi,t) = f(r)A(\theta,\phi,t) = \frac{1}{r^2}\delta(r-r_n)A(\theta,\phi,t),$$

$$A(\theta,\phi,t)=Y(\theta,\phi)k(t).$$

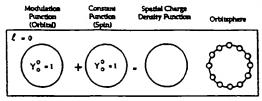
- In these cases, the spherical harmonic function correspond to a traveling charge-density wave confined to the spherical
- 5 shell which gives rise to the phenomenan of the sital angular momentum. The orbital functions which a pollulate the con-
- 7 stant "spin" function shown granticals in 1.1g. 3 are given in the "Angular Functions" section.

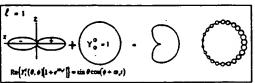
3. Spin function

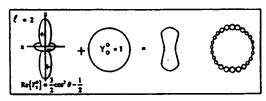
The orbitsplace sain function comprises a constant

11 charge-density fulfiction with moving charge confined to
a two-dimensional spherical shell. The current pattern of
the orbitsphere spin function comprises an infinite series of correlated orthogonal great circle current loops
wherein each point moves time harmonically with angular
velocity

$$\omega_n = \frac{\hbar}{m_n r^2}.$$
 (8)







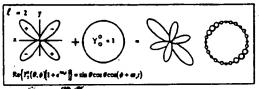


Fig. 2220 orbital function modulates the constant (spin) function from fig. 0; cross-sectional view).

The current pattern is generated over the surface by a cries of nested rotations of two orthogonal great circle current loops where the coordinate axes rotate with the two orthogonal great circles. Half of the pattern is generated as the z-axis rotates to the negative z-axis during a 1st set of nested rotations. The mirror image, second half of the pattern is generated as the z-axis rotates back to its original direction during a 2nd set of nested rotations.

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3.1. Points on great circle current loop one

$$\begin{bmatrix} x_1 \\ y_1 \\ z_1 \end{bmatrix} =$$

$$\begin{bmatrix} \cos(\Delta \alpha) & -\sin^2(\Delta \alpha) & -\sin(\Delta \alpha)\cos(\Delta \alpha) \\ 0 & \cos(\Delta \alpha) & -\sin(\Delta \alpha) \\ \sin(\Delta \alpha) & \cos(\Delta \alpha)\sin(\Delta \alpha) & \cos^2(\Delta \alpha) \end{bmatrix} \begin{bmatrix} x_1' \\ y_1' \\ z_1' \end{bmatrix}$$
(9)

and
$$\Delta \alpha' = -\Delta \alpha$$
 replaces $\Delta \alpha$ for $\sum_{n=1}^{\sqrt{2}\pi/\Delta \alpha} \Delta \alpha = \sqrt{2}\pi$; $\sum_{n=1}^{\sqrt{2}\pi/\Delta \alpha'} |\Delta \alpha'| = \sqrt{2}\pi$.

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3.2. Points on great circle current loop two

$$\begin{bmatrix} x_2 \\ y_2 \\ z_2 \end{bmatrix} = \begin{bmatrix} \cos(\Delta \pi) & \sin^2(\Delta \pi) & \sin(\Delta \pi) \end{bmatrix}$$

$$\begin{bmatrix} \cos(\Delta\alpha) & -\sin^2(\Delta\alpha) & -\sin(\Delta\alpha)\cos(\Delta\alpha) \\ 0 & \cos(\Delta\alpha) & -\sin(\Delta\alpha) \\ \sin(\Delta\alpha) & \cos(\Delta\alpha)\sin(\Delta\alpha) & \cos^2(\Delta\alpha) \end{bmatrix} \begin{bmatrix} x_2' \\ y_2' \\ z_2' \end{bmatrix}$$
(10)

and $\Delta \alpha' = -\Delta \alpha$ replaces $\Delta \alpha$ for $\sum_{n=1}^{\sqrt{2}\pi/\Delta \alpha} \Delta \alpha = \sqrt{2}\pi$; $\sum_{n=1}^{\sqrt{2}\pi/\Delta \alpha'} |\Delta \alpha'| = \sqrt{2}\pi$.

The orbitsphere is given by reiterations of Eqs. (9) and (10). The output given by the nonprimed coordinates is the input of the next iteration corresponding to each successive 29 nested rotation by the infinitesimal angle where the summation of the rotation about each of the x-axis and the y-axis is

9 $\sum_{m=1}^{\sqrt{2}\pi/\Delta e} \Delta \alpha = \sqrt{2}\pi$ (1st set) and $\sum_{m=1}^{\sqrt{2}\pi/|\Delta \alpha'|} |\Delta \alpha'| = \sqrt{2}\pi$ (2nd set). The current pattern corresponding to great circle current loop one and two shown with 8.49° increments of the

current loop one and two shown with 8.49° increments of the infinitesimal angular variable Δα(Δα') of Eqs. (9) and (10)
 is shown from the perspective of looking along the z-axis

in Fig. 2. The true orbitsphere current pattern is given as $\Delta\alpha(\Delta\alpha')$ approaches zero. This current pattern gives rise to

the phenomenon corresponding to the spin quantum number

17 of the electron.

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4. Magnetic field equations of the electron

The orbitsphere is a shell of negative charge current comprising correlated charge motion along great circles. For

21 \(\lambda = 0 \), the orbitsphere gives rise to a magnetic moment 1 Bohr magneton [3].

$$\mu_{\rm B} = \frac{e\hbar}{2m_{\rm o}} = 9.274 \times 10^{-24} \, {\rm JT}^{-1}.$$

23 The magnetic field of the electron shows a figure is given by

$$H = \frac{e\hbar}{m_e r_e^2} (i_e \cos \theta - i_e \sin \theta)$$
 (12)

$$H = \frac{e\hbar}{2m_{e}r^{3}}(1.2\cos\theta - 1.500) r_{n}. \tag{13}$$

25 The energy stored in the manner field of the electron is

$$E_{\text{mag}} = \frac{1}{2} \mu_0 \int_0^{2\pi} \int_0^{2\pi} d\theta \, d\theta \, d\theta \, d\theta, \qquad (14)$$

$$E_{\text{mag total}} = \frac{n\mu_0 e^2 T^{-1}}{m^2} \tag{15}$$

5. Stern-Gerlach experiment

27 The Stern-Gerlach experiment implies a magnetic moment of one Bohr magneton and an associated angular

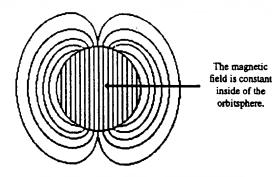


Fig. 4. The magnetic field of an electron orbitsphale

momentum quantum number of 1/2. However, this quantum number is called the spin quantum number, s ($s = \frac{1}{2}$; $m_s = \pm \frac{1}{2}$). The superposition of the actor projection of the orbitsphere angular grown in on to an axis S that precesses about the z-axis called the spin axis at an angle of $\theta = \pi/3$ and an angle of π with respect to $\langle L_{xy} \rangle_{\sum \Delta x}$ is

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$$S = \pm \sqrt{\frac{3}{4}} \hbar. \tag{16}$$

S rotates about the z-axis at the Larmor frequency. $\langle S_z \rangle$, the time averaged projection of the orbitsphere angular momentum ongo the axis of the applied magnetic field is

$$(1) \Sigma = \pm \frac{1}{2}$$
 (17)

Electron g factor

Conservation of angular momentum of the orbitsphere permits a discrete change of its kinetic angular momentum $(r \times mv)$ by the applied magnetic field of $\hbar/2$, and concomitantly the potential angular momentum $(r \times eA)$ must change by $-\hbar/2$.

$$\Delta \mathbf{L} = \frac{\hbar}{2} - \mathbf{r} \times \epsilon \mathbf{A} \tag{18}$$

$$= \left[\frac{\hbar}{2} - \frac{e\phi}{2\pi}\right]\hat{z}. \tag{19}$$

In order that the change of angular momentum, ΔL , equals zero, ϕ must be $\Phi_0 = h/2e$, the magnetic flux quantum. The magnetic moment of the electron is parallel or antiparallel to the applied field only. During the spin-flip transition, power must be conserved. Power flow is governed by the Poynting power theorem,

$$\nabla \bullet (\mathbf{E} \times \mathbf{H}) = -\frac{\partial}{\partial t} \left[\frac{1}{2} \mu_0 \mathbf{H} \bullet \mathbf{H} \right]$$
$$-\frac{\partial}{\partial t} \left[\frac{1}{2} \epsilon_0 \mathbf{E} \bullet \mathbf{E} \right] - \mathbf{J} \bullet \mathbf{E}$$
(20)

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Eq. (21) guires the total energy of the flip transition which is the sum of the energy of reorientation of the magnetic

moment (1st term), the magnetic energy (2nd term), the electric energy (3rd term), and the dissipated energy of a

fluxon treading the orbitsphere (4th term), respectively,

$$\Delta E_{\text{mag}}^{\text{spin}} = 2\left(1 + \frac{\alpha}{2\pi} + \frac{2}{3}\alpha^2\left(\frac{\alpha}{2\pi}\right) - \frac{4}{3}\left(\frac{\alpha}{2\pi}\right)^2\right)\mu_{\text{B}}B, (21)$$

$$\Delta E_{\text{mag}}^{\text{opin}} = g\mu_{\text{B}}B,\tag{22}$$

where the stored magnetic energy corresponding to the $\partial/\partial t[\frac{1}{2}\mu_0\mathbf{H} \bullet \mathbf{H}]$ term increases, the stored electric energy corresponding to the $\partial/\partial t[\frac{1}{2}\epsilon_0\mathbf{E} \bullet \mathbf{E}]$ term increases, and

9 the J • E term is dissipative. The spin-flip transition can be considered as involving a magnetic moment of g times that

of a Bohr magneton. The g factor is redesignated the fluxon g factor as opposed to the anomalous g factor. The calcu-

lated value of g/2 is 1.001159652137. The experimental value [4] of g/2 is 1.001159652188(4).

7. Angular functions

The time, radial, and angular solutions of the wave equation are separable. Also based on the radial solution, the angular charge and current-density functions of the electron.

19 $A(\theta, \phi, t)$, must be a solution of the wave equation in two dimensions (plus time),

$$\left[\nabla^2 - \frac{1}{v^2} \frac{\partial^2}{\partial t^2}\right] A(\theta, \phi, t) = 0, \tag{23}$$

where $\rho(r, \theta, \phi, t) = f(r)A(\theta, \phi, t) = (1/r^2)\delta(r - r_n)A(\theta, \phi, t)$ synchronous with waves traveling at the speed of light [2]. and $A(\theta, \phi, t) = Y(\theta, \phi)k(t)$ (See Instability of Excited States' section.)

$$\left[\frac{1}{r^2\sin\theta}\frac{\partial}{\partial\theta}\left(\sin\theta\frac{\partial}{\partial\theta}\right)_{r,\phi} + \frac{1}{r^2\sin^2\theta}\left(\frac{\partial^2}{\partial\phi^2}\right)_{r,\phi}\right]$$

$$-\frac{1}{v^2}\frac{\partial^2}{\partial t^2}\bigg]A(\theta,\phi,t)=0,$$

23 where v is the linear velocity of electron. The charge-density functions including the time function factor

. ._ 0

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$$\rho(r,\theta,\phi,t) = \frac{e}{8\pi \pi} [\delta(r-r)] + \gamma_0^0(\theta,\phi) + \gamma_0^0(\theta,\phi)]. \quad (25)$$

$$\ell > 0$$
,

$$\rho(r, \theta, \phi, t) = \frac{\ell}{4\pi r^2} [\delta(r - r_n)] [Y_0^0(\theta, \phi)]$$

$$+Re\{Y_{\ell}^{m}(\theta,\phi)[1+e^{i\omega_{n}\ell}]\}\},$$
 (26)

 $Re\{Y_{\ell}^{m}(\theta,\phi)[1 + e^{i\omega_{n}t}]\} = Re\{Y_{\ell}^{m}(\theta,\phi) + Y_{\ell}^{m}(\theta,\phi)e^{i\omega_{n}t}\}$ $= P_{\ell}^{m}(\cos\theta)\cos m\phi + P_{\ell}^{m}(\cos\theta)\cos(m\phi + \omega_{n}t) \text{ and } \omega_{n} = 0$ for m = 0.

8. Spin and orbital parameters

The total function that describes the spinning motion of each electron orbitsphere is composed of two functions. One function, the spin function, is spatially uniform over the orbitsphere, spins with a quantized angular velocity, and gives rise to spin angular momentum. The other function, the modulation function, can be spatially uniform in which case there is no orbital angular momentum and the magnetic moment of the electron orbitsphere is one Bohr magneton or not spatially uniform in which case there is orbital angular momentum. The modulation function also rotates with a quantized angular velocity.

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The spin function of the electron corresponds to the nonradiative n = 1, $\ell = 0$ state of atomic hydrogen which is well known as an s state or orbital. (See Fig. 18 100) in tharge function and Fig. 2 for the current function.) Post orbitals with the & quantum number not equal to the constant spin function is modulated by a time and spherical harmonic function as given by Eq. (26) and shown in Fig. 3. The modulation or traveling charge density wave corresponds to an orbital angular momentum in addition to a spin angular momentum. These states are varically referred to as p, d, f, etc. orbitals. Application of Haus's [2] condition also predicts nonradiation for a constant spin function modulated by a time and splerically harmonic orbital function. There is acceleration without radiation. (Also see Abbott and Griffiths and Goedecke (5,68) However, in the case that such a state ariseties an excited state by photon absorption, it is radiative singe it possesses spacetime Fourier Transform components (See Instability of Excited States" section.)

8.1. Moment of inertia and spin and rotational energies

l = 0,

$$I_z = I_{\text{pin}} = \frac{m_0 r_a^2}{2},\tag{27}$$

$$L_{i} = I\omega l_{c} = \pm \frac{\hbar}{2}, \tag{28}$$

$$E_{\text{rotational}} = E_{\text{rotational, spin}} = \frac{1}{2} \left[I_{\text{spin}} \left(\frac{\hbar}{m_0 r_n^2} \right)^2 \right]$$

$$= \frac{1}{2} \left[\frac{m_{\rm e} r_{\rm n}^2}{2} \left(\frac{\hbar}{m_{\rm e} r_{\rm n}^2} \right)^2 \right] = \frac{1}{4} \left[\frac{\hbar^2}{2I_{\rm spin}} \right]. \tag{29}$$

$$I_{\text{orbital}} = m_{\text{e}} r_{\text{a}}^2 \left[\frac{\ell(\ell+1)}{\ell^2 + \ell + 1} \right]^{1/2},$$
 (30)

$$I_{-} = m\hbar. \tag{31}$$

$$L_{\text{r total}} = L_{\text{r spin}} + L_{\text{r orbital}}, \tag{32}$$

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$$E_{\text{routional, orbital}} = \frac{\hbar^2}{2I} \left[\frac{\ell(\ell+1)}{\ell^2 + 2\ell + 1} \right], \tag{33}$$

$$T = \frac{\hbar^2}{2m_e r_n^2},\tag{34}$$

$$\langle E_{\text{rotational, orbital}} \rangle = 0.$$
 (35)

From Eq. (35), the time average rotational energy is zero; thus, the principal levels are degenerate except when a mag-3 netic field is applied.

9. Nonradiation condition (acceleration without radiation)

The Fourier transform of the electron charge-density function is a solution of the four-dimensional wave equation in frequency space $(k, \omega space)$. Then the corresponding Fourier transform of the current-density function $K(s,\Theta,\Phi,\omega)$ is given by multiplying by the constant angu-11 lar frequency.

$$K(s, \Theta, \Phi, \omega) = 4\pi\omega_n \frac{\sin(2s_n r_n)}{2s_n r_n} \otimes 2\pi \sum_{n=1}^{\infty}$$

$$\times \frac{(-1)^{n-1}(\pi\sin\theta)^{2(n-1)}}{(\nu-1)!(\nu-1)!} \frac{\Gamma(\frac{1}{2})\Gamma(\nu+\frac{1}{2})}{(\pi\cos\theta)^{2n+1}2^{n+1}} \frac{2\nu!}{(\nu-1)!} s^{-2n},$$
(36)

$$\otimes 2\pi \sum_{v=1}^{\infty} \frac{(-1)^{v-1} (\pi \sin \Phi)^{2(v-1)}}{(v-1)! (v-1)!} \frac{\Gamma(\frac{1}{2}) \Gamma(v+\frac{1}{2})}{(\pi \cos \Phi)^{2v+1} 2^{v+1}}$$

$$\times \frac{2v!}{(v-1)!} s^{-2v} \frac{1}{4\pi} [\delta(\omega-\omega_n) + \delta(\omega+\omega_n)]_{s}$$

 $s_n \bullet v_n = s_n \bullet c = \omega_n$ implies $r_n = \lambda_n$ Spacetime had of $\omega_n/c = k$ or $\omega_n/c\sqrt{\epsilon/\epsilon_0} = k$ for which the I form of the current-density function is nonzer

15 Radiation due to charge motion does medium when this boundary conditions the is also determined from the fields beard in any

is also determined from the fields based laxwell's equa-

10. Force balance equati

The radius of the profile lative (n = 1) state to the electron part of force equations of Maxwell relating the electron again the angular 21 ing the electronical the charge and make consity functions wherein the angular

momentum of the effection is given by Planck's constant bar. 23 The reduced mass arises naturally from an electrodynamic

interaction between the electron and the proton.

$$\frac{m_{\rm e}}{4\pi r_1^2} \frac{v_1^2}{r_1} = \frac{e}{4\pi r_1^2} \frac{Ze}{4\pi e_0 r_1^2} - \frac{1}{4\pi r_1^2} \frac{\hbar^2}{mr_n^3},\tag{37}$$

$$r_1 = \frac{a_H}{Z}. (38)$$

11. Energy calculations

From Maxwell's equations, the potential energy V, kinetic energy T, electric energy or binding energy $E_{\rm ele}$ are

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$$V = \frac{-Ze^2}{4\pi\epsilon_0 r_1} = \frac{-Z^2e^2}{4\pi\epsilon_0 a_H} = -Z^2 \times 4.3675 \times 10^{-18} \,\text{J}$$

$$=-Z^2 \times 27.2 \text{ eV},$$
 (39)

$$T = \frac{Z^2 e^2}{8\pi \epsilon_0 a_H} = Z^2 \times 13.59 \text{ eV}, \tag{40}$$

$$T = E_{\text{ch}} = -\frac{1}{2} \epsilon_0 \int_{-\infty}^{r_1} \mathbf{E}^2 \, dv \text{ where } \mathbf{E} = -\frac{Ze}{4\pi\epsilon_0 r_{\perp}^2}, \quad (41)$$

$$E_{\rm che} = -\frac{Z^2 e^2}{8\pi\epsilon_0 a_H} = -Z^2 \times 2.1786 \times 10^{-18} \, \text{J}$$

$$=-Z^2 \times 13.598 \text{ eV}.$$
 (42)

The calculated Rydberg constant experimental Rydberg constant is 19,67

12. Excited states

CQM gives closed real solutions for the resonant photons and excited state electron anctions. The angular momentum of the photolic gives by

$$\mathbf{m} = \frac{1}{2} \operatorname{Re}[\mathbf{r} * (\mathbf{B} \times \mathbf{B}^*)] = \hbar \tag{43}$$

conserved [7, pp. 739-779]. The change in angular ve-ty of the electron is equal to the angular frequency of the respnant photon. The energy is given by Planck's equathe predicted energies, Lamb shift, hyperfine structure, conant line shape, line width, selection rules, etc. are in agreement with observation.

The orbitsphere is a dynamic spherical resonator cavity which traps photons of discrete frequencies. The relationship between an allowed radius and the photon standing wave wavelength is

$$2\pi r = n\lambda \tag{44}$$

where π is an integer. The relationship between an allowed radius and the electron wavelength is

$$2\pi(nr_1) = 2\pi r_n = n\lambda_1 = \lambda_n, \tag{45}$$

where n = 1, 2, 3, 4, The radius of an orbitsphere increases with the absorption of electromagnetic energy. The radii of excited states are solved using the electromagnetic force equations of Maxwell relating the field from the charge of the proton, the electric field of the photon, and chargeand mass-density functions of the electron wherein the angular momentum of the electron is given by Planck's constant bar (Eq. (37)). The solutions to Maxwell's equations for modes that can be excited in the orbitsphere resonator cavity give rise to four quantum numbers, and the energies of the modes are the experimentally known

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hydrogen spectrum. The relationship between the electric field equation and the trapped photon source charge-density

function is given by Maxwell's equation in two dimensions.

$$\mathbf{n} \bullet (\mathbf{E}_1 - \mathbf{E}_2) = \frac{\sigma}{c_1}. \tag{46}$$

The photon standing electromagnetic wave is phase matched with the electron

$$E_{r \text{ photons } a,l,m} = \frac{e(na_H)^l}{4\pi\epsilon_0} \frac{1}{r^{(l+2)}} \left[-Y_0^0(\theta,\phi) + \frac{1}{n} [Y_0^0(\theta,\phi) + Re\{Y_l^m(\theta,\phi)[1 + e^{i\alpha a_l t}]\}] \right] \delta(r - r_a), \quad (47)$$

$$\omega_n = 0$$
 for $m = 0$,

$$\ell=1,2,\ldots,n-1,$$

$$m = -\ell, -\ell + 1, \dots, 0, \dots, +\ell,$$

$$E_{r \text{ total}} = \frac{e}{4\pi\epsilon_0 r^2} + \frac{e(na_H)^r}{4\pi\epsilon_0} \frac{1}{r^{(\ell+2)}} \left[-Y_0^0(\theta, \phi) + \frac{1}{n} [Y_0^0(\theta, \phi) + \frac{1}{n} [Y_0^0(\theta, \phi)] + Re\{Y_\ell^0(\theta, \phi)[1 + e^{i\alpha_0 \ell}]\}] \right] \delta(r - r_n),$$
(48)

 $\omega_n = 0$ for m = 0.

For $r = na_H$ and m = 0, the total radial electric field is

$$\mathbf{E}_{r \text{ total}} = \frac{1}{n} \frac{e}{4\pi e_0 (na_H)^2}.$$
 (49)

The energy of the photon which excites a mode in the electron spherical resonator cavity from radius an to radius

$$E_{\rm photon} = \frac{e^2}{8\pi\epsilon_0 a_H} \left[1 - \frac{1}{n^2} \right] = hv = \hbar\omega.$$

The change in angular velocity of the orbits

$$\Delta \omega = \frac{\hbar}{m_e(a_H)^2} - \frac{\hbar}{m_e(na_H)^2} = \frac{\hbar}{m_e(a_H)^2}$$
 (51)

$$\frac{1}{2}m_e(\Delta v)^2 = \frac{e^2}{8\pi\epsilon_0 d_H} \left[1 - \frac{1}{2\pi} \right] \tag{52}$$

The change in angular process to one electron orbitsphere is identical to the angular locity of the photon necessary for the excitation and the contraspondence principle holds. It can be demonstrate that the resonance condition between

these frequencies in to be satisfied in order to have a net change of the energy field [8].

13. Orbital and spin splitting

The ratio of the square of the angular momentum, M^2 , to the square of the energy, U^2 , for a pure (ℓ, m) multipole is [7, pp. 739-752]

$$\frac{M^2}{U^2} = \frac{m^2}{\omega^2}. (53)$$

The magnetic moment is defined as

$$\mu = \frac{\text{charge} \times \text{angular momentum}}{2 \times \text{mass}}.$$
 (54)

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The radiation of a multipole of order (I, m) carries mh units of the z component of angular momentum per photon of energy $\hbar\omega$. Thus, the z component of the angular momentum of the corresponding excited state electron orbitsphere is

 $L_2 = m\hbar$.

Therefore

$$\mu_e = \frac{emh}{2m_e} = m\mu_B, \tag{56}$$

orbital splitting energy where $\mu_{\rm B}$ is the Bohr magneton. The

$$E_{\text{max}}^{\text{orb}} = m\mu_{\text{B}}B. \tag{57}$$

enterpies superimpose; thus, the The spin and orbital spitting principal excited staff rgy levels of the hydrogen atom are split by the

$$E_{max}^{\text{constant}} = \frac{\hbar}{m_b} B m_s g \frac{e\hbar}{m_b} B \text{ where}$$
 (58)

$$\mathbf{m} = -\ell, -\ell+1, \ldots, 0, \ldots, +\ell,$$

$$m_s = \pm \frac{1}{2}$$
.

For the electric dipole transition, the selection rules are

$$\Delta m = 0, \pm 1, \tag{59}$$

 $\Delta m_s = 0.$

14. Resonant line shape and lamb shift

The spectroscopic linewidth shown in Fig. 5 arises from the classical rise-time band-width relationship, and the Lamb shift is due to conservation of energy and linear momenturn and arises from the radiation reaction force between the electron and the photon. It follows from the Poynting power theorem with spherical radiation that the transition probabilities are given by the ratio of power and the energy of the transition [7, pp. 758-763]. The transition probability in the

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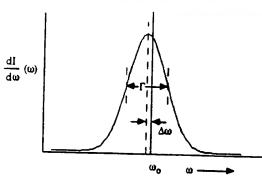


Fig. 5. Broadening of the spectral line due to the rise-time and shifting of the spectral line due to the radiative reaction. The resonant line shape has width Γ . The level shift is $\Delta \omega$.

1 case of the electric multipole moment is

$$\frac{1}{r} = \frac{\text{power}}{\text{energy}},\tag{60}$$

$$\frac{1}{\tau} = \frac{\left[\frac{2m\pi}{((2l+1)!!)^2} \left(\frac{l+1}{l}\right) k^{2l+1} | Q_{lm} + Q'_{lm}|^2\right]}{[\hbar \omega]}$$

$$= 2\pi \left(\frac{e^2}{h}\right) \sqrt{\frac{\mu_0}{\epsilon_0}} \frac{2\pi}{[(2l+1)!!)^2} \left(\frac{l+1}{l}\right)$$

$$\times \left(\frac{3}{l+3}\right)^2 (kr_n)^{2l} \omega, \tag{61}$$

$$\mathbb{E}(\omega) \propto \int_0^\infty \mathrm{e}^{-\alpha t} \mathrm{e}^{-\mathrm{i} \omega t} \, \mathrm{d}t = \frac{1}{\alpha - \mathrm{i} \omega}.$$

The relationship between the rise-time and there for exponential decay is

$$\tau \Gamma = \frac{1}{\pi}.\tag{63}$$

The energy radiated per unit frequency enterval is

$$\frac{\mathrm{d}I(\omega)}{\mathrm{d}\omega} = I_0 \frac{\Gamma}{2\pi} \frac{\Gamma}{(\omega - \omega_0 - \Delta\omega)^{2/3} \Gamma(\Gamma/2)^{2/3}}.$$
 (64)

15. Lamb stift

The Lamb shift of the ²P_{1/2} state of the hydrogen atom is due to conservation of linear momentum of the electron, atom, and photon. The electron component is

$$_{9}$$
 $\Delta f = \frac{\Delta \omega}{2\pi} = \frac{E_{h\tau}}{h} = 3\frac{(E_{h\tau})^2}{h2m_ec^2} = 1052 \text{ MHz},$ (65)

where Em is

$$E_{hv} = 13.6 \left(1 - \frac{1}{n^2} \right) \frac{1}{|X_{lm}|_{L_{ml}}^2} - h \Delta f, \tag{66}$$

$$E_{hr} = 13.6 \left(1 - \frac{1}{n^2} \right) \frac{3}{8\pi} - h \Delta f, \tag{67}$$

$$h\Delta f < < 1. \tag{68}$$

Therefore,

$$E_{hr} = 13.6 \left(1 - \frac{1}{n^2} \right) \frac{3}{8\pi}. \tag{69}$$

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The atom component is

$$\Delta f = \frac{\Delta \omega}{2\pi} = \frac{E_{hv}}{h} = \frac{1}{2} \frac{(E_{hv})^2}{2m_H c^2} = 6.5 \text{ MHz}$$
(70)

The sum of the components is

$$\Delta f = 1052 \text{ MHz} + 6.5 \text{ MHz} = 100.5 \text{ MHz}$$
 (71)

The experimental Lamb sing in 10.3 MHz

16. Instability of excilenstates

For the expited energy states of the hydrogen atom, $\sigma_{\rm photos}$, the two dimensional surface charge due to the trapped photons and elegation orbitsphere, given by Eqs. (46) and (47)

$$= \frac{e}{4\pi(r_n)^2} \left[Y_0^0(\theta, \phi) - \frac{1}{n} [Y_0^0(\theta, \phi) + Re\{Y_\ell^m(\theta, \phi)[1 + e^{i\alpha_n t}]\}] \right] \delta(r - r_n), \tag{72}$$

where n = 2, 3, 4, ..., Whereas, σ_{electron} , the two-dimensional surface charge of the electron orbitsphere given by Eq. (26) is

$$\sigma_{\text{electron}} = \frac{-\sigma}{4\pi(r_a)^2} [Y_0^0(\theta, \phi) + Re\{Y_r^m(\theta, \phi)[1 + e^{im_a t}]\}] \delta(r - r_a).$$
 (73)

The superposition of $\sigma_{\rm photon}$ (Eq. (72)) and $\sigma_{\rm electron}$ is equivalent to the sum of a radial electric dipole represented by a doublet function and a radial electric monopole represented by a delta function.

 $\sigma_{\rm photon} + \sigma_{\rm electron}$

$$= \frac{e}{4\pi(r_n)^2} \left[Y_0^0(\theta, \phi) \delta(r - r_n) - \frac{1}{n} Y_0^0(\theta, \phi) \delta(r - r_n) - \left(1 + \frac{1}{n}\right) \left[Re\{Y_\ell^m(\theta, \phi)[1 + e^{i\omega_n t}]\} \right] \delta(r - r_n) \right],$$
(74) 27

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where $n = 2, 3, 4, \dots$. Due to the radial doublet, excited states are radiative since spacetime harmonics of $\omega_n/c = k$ or $(\omega_n/c)\sqrt{\epsilon/\epsilon_0} = k$ do exist for which the spacetime Fourier

or $(\omega_{\gamma}/c)\sqrt{\epsilon/\epsilon_0} = k$ do exist for which the spacetime round transform of the current-density function is nonzero.

17. Photon equations

The time-averaged angular-momentum density, m, of an emitted photon is

$$\mathbf{m} = \frac{1}{8\pi} Re[\mathbf{r} \times (\mathbf{E} \times \mathbf{B}^*)] = \hbar. \tag{75}$$

A linearly polarized photon orbitsphere is generated from two orthogonal great circle field lines shown in Fig. 6 rather

than two great circle current loops as in the case of the electron spin function. The right-handed circularly polar-

ized photon orbitsphere shown in Fig. 7 corresponds to the l3 case wherein the summation of the rotation about each of

case wherein the summation of the rotation about each of the x-axis and the y-axis is ∑_{x=1}^{√2x/Δα} Δα = √2π, and the mirror image left-handed circularly polarized photon orbitsphere corresponds to the case wherein the summation

of the rotation about each of the x-axis and the y-axis is $\sum_{n=1}^{\sqrt{2}\pi/|\Delta\alpha'|} |\Delta\alpha'| = \sqrt{2}\pi.$

 17.1. Nested set of great circle field lines generates the photon function

21 H Field

$$\begin{bmatrix} x_1 \\ y_1 \\ z_1 \end{bmatrix} =$$

$$\begin{bmatrix} \cos(\Delta\alpha) & -\sin^2(\Delta\alpha) & -\sin(\Delta\alpha)\cos(\Delta\alpha) \\ 0 & \cos(\Delta\alpha) & -\sin(\Delta\alpha) \\ \sin(\Delta\alpha)\cos(\Delta\alpha)\sin(\Delta\alpha) & \cos^2(\Delta\alpha) \end{bmatrix}$$

and $\Delta \alpha' = -\Delta \alpha$ replaces $\Delta \alpha$ for $\Delta \alpha = \sqrt{2\pi}$

 $\sum_{n=1}^{\sqrt{2}\pi/|\Delta\alpha'|} |\Delta\alpha'| = \sqrt{2}\pi.$ E Field

$$\begin{bmatrix} z_2 \end{bmatrix} \begin{bmatrix} \cos(\Delta \alpha) & \sin(\Delta \alpha) & -\sin(\Delta \alpha)\cos(\Delta \alpha) \\ 0 & \cos(\Delta \alpha) & -\sin(\Delta \alpha) \\ \sin(\Delta \alpha) & \cos(\Delta \alpha)\sin(\Delta \alpha) & \cos^2(\Delta \alpha) \end{bmatrix} \begin{bmatrix} x_2' \\ y_2' \\ z_2' \\ z_2' \end{bmatrix}$$

25 and $\Delta \alpha' = -\Delta \alpha$ replaces $\Delta \alpha$ for $\sum_{n=1}^{\sqrt{2}\pi/\Delta \alpha} \Delta \alpha = \sqrt{2}\pi$; $\sum_{n=1}^{\sqrt{2}\pi/\Delta \alpha'} |\Delta \alpha'| = \sqrt{2}\pi$

 $\sum_{n=1}^{\sqrt{2\pi}/|\Delta\alpha'|} |\Delta\alpha'| = \sqrt{2\pi}.$ The field lines in the lab frame follow from the relativistic invariance of charge as given by Purceil [9]. The relationship

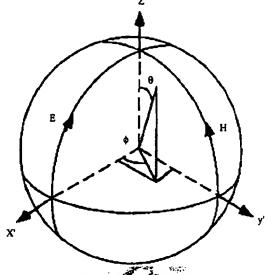
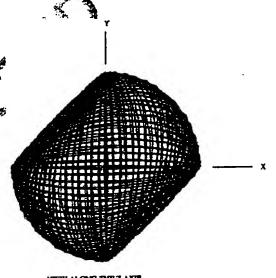


Fig. 6. The Cartesian coordinate wherein the first great circle magnetic field line. It is in the yz-plane, and the second great circle electric field line as in the xx plane is designated the photon orbitsphere reference frame of a photon orbitsphere.



VIEW ALONG THE 2 AXIS

Fig. 7. The field line pattern from the perspective of looking along the z-axis of a right-handed circularly polarized photon.

between the relativistic velocity and the electric field of a moving charge shown schematically in Fig. 8. From Eqs. (76)-(77) with $\sum_{n=1}^{\sqrt{2}\pi/\Delta n} \Delta \alpha = \sqrt{2}\pi$, the photon equation in the lab frame of a right-handed circularly polarized

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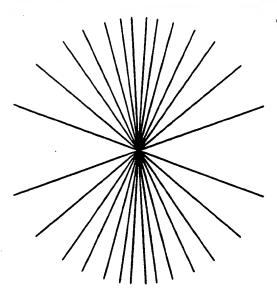


Fig. 8. The electric field of a moving point charge ($v = \frac{4}{3}c$).

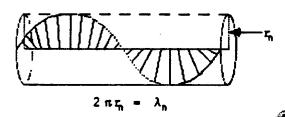


Fig. 9. The electric field lines of a right-handed circularly polarize photon orbitsphere as seen along the axis of propagation inertial reference frame as it passes a fixed point.

photon orbitsphere is

$$E = E_0[x + iy]e^{-jA_0t}e^{-jast},$$
 (78)

$$H = \left(\frac{E_0}{\eta}\right) [y - ix]e^{-jA_0x}e^{-jaux} = E_0 \sqrt{1 - ix}]e^{-jA_0x}e^{-jaux}$$
(79)

with a wavelength of
$$\lambda = 2\pi \frac{c}{\omega}$$
. (80)

The relationship the photon orbitsphere radius and wavelength

$$2\pi r_0 = \lambda_0. \tag{81}$$

- The electric field lines of a right-handed circularly polarized photon orbitsphere as seen along the axis of propagation in
- the lab inertial reference frame as it passes a fixed point is shown in Fig. 9.

17.2. Spherical wave

Photons superimpose, and the amplitude due to N photons

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 $\mathbf{E}_{\text{total}} = \sum_{r=1}^{N} \frac{\mathrm{e}^{-\mathrm{i}\mathbf{r}_{r}|\mathbf{r}-\mathbf{r}'|}}{4\pi|\mathbf{r}-\mathbf{r}'|} f(\theta,\phi).$ (82)

In the far field, the emitted wave is a spherical wave

$$\mathbf{E}_{\text{total}} = \mathbf{E}_0 \frac{e^{-i\mathbf{k}\mathbf{r}}}{r}.\tag{83}$$

The Green Function is given as the solution of the wave equation. Thus, the superposition of photons gives the classical result. As r goes to infinity, the spherical comes a plane wave. The double slit interference predicted. From the equation of a photon, a duality arises naturally. The energy is riven by Planck's equation; yet, an interfere when photons add over time or s

18. Equations of the free

18.1. Charge-densit four

The radius of the electron orbitsphere increases with the absorption dielectron magnetic energy [10]. With the absorpenergy exactly equal to the ionization fon becomes ionized and is a plane wave ve in the limit) with the de Broglie wave-The ionized electron traveling at constant velocity idiative and is a two-dimensional surface having a al charge of e and a total mass of m_e . The solution of the bundary value problem of the free electron is given by the projection of the orbitsphere into a plane that linearly propagates along an axis perpendicular to the plane where the velocity of the plane and the orbitsphere is given by

$$v = \frac{\hbar}{m_e \rho_0} \tag{84}$$

and the radius of the orbitsphere in spherical coordinates is equal to the radius of the free electron in cylindrical coordinates $(\rho_0 = r_0)$. The mass-density function of a free electron shown in Fig. 10 is a two-dimensional disk having the mass-density distribution in the $xy(\rho)$ -plane

$$\rho_m(\rho,\phi,z) = \frac{m_0}{\frac{1}{2}\pi\rho_0^2}\pi\left(\frac{\rho}{2\rho_0}\right)\sqrt{\rho_0^2 - \rho^2}\delta(z) \tag{85}$$

and charge-density distribution, $\rho_{\bullet}(\rho, \phi, z)$, in the xy-plane given by replacing me with e. The charge-density distribution of the free electron has recently been confirmed experimentally [11,12]. Researchers working at the Japanese National Laboratory for High Energy Physics (KEK) demonstrated that the charge of the free electron increases toward the particle's core and is symmetrical as a function of ϕ . In addition, the wave-particle duality arises naturally,

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Increasing electron density ----

Front View of Electron

$$\rho_0 = \frac{1}{mv_0}$$
electron moving in this direction



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Side View of Electron

Fig. 10. The front view of the magnitude of the mass (charge) density funcof a free electron; side view of a free electron along the axis of propagation - z-axis.

- and the result is consistent with scattering experiments from Substitution of me for e in Eq. (87) followed by substitu-1 helium and the double split experiment [1].
- 18.2. Current-density function 3

Consider an electron initially bound as ar radius $r = r_0 = r_0$ ionized from a hydro vith the magnitude of the angular velocity of the is given 7

$$\omega = \frac{\hbar}{m_0 r^2}. ag{86}$$

of the free electron propagating The current-density fu in the inertial frame of the with velocity of along proton is given by xy-plane as the a div r projection of the current into increases from $r = r_0$ to $r = \infty$. The current-deficity function of the free electron, is

$$\mathbf{J}(\rho,\phi,z,t) = \begin{bmatrix} \frac{\rho}{\pi} \left(\frac{\rho}{2\rho_0} \right) \frac{e}{\frac{\epsilon}{3}\pi\rho_0^3} \frac{\hbar}{m_0\sqrt{\rho_0^2 - \rho^2}} \mathbf{i}_{\phi} \end{bmatrix}, \tag{87}$$

where $\rho_0 = r_0$. The angular momentum, L, is given by 13

$$\mathbf{Li}_{\mathbf{s}} = m_{\mathbf{s}} r^2 \omega. \tag{88}$$

tion into Eq. (88) gives the angular momentum density function, L

$$Li_{a} = \pi \left(\frac{\rho}{2\rho_{0}}\right) \frac{m_{0}}{\frac{4}{3}\pi\rho_{0}^{3}} \frac{\hbar}{m_{0}\sqrt{\rho_{0}^{2} - \rho^{2}}} \rho^{2}.$$
 (89)

The total angular momentum of the free electron is given by integration over the two-dimensional disk having the angular momentum density given by Eq. (89).

$$\text{Li}_{z} = \int_{0}^{2\pi} \int_{0}^{\rho_{0}} \pi \left(\frac{\rho}{2\rho_{0}}\right) \frac{m_{e}}{\frac{4}{3}\pi\rho_{0}^{3}} \frac{\hbar}{m_{e}\sqrt{\rho_{0}^{2} - \rho^{2}}} \rho^{2} \rho \, d\rho \, d\phi = \hbar. \tag{90}$$

The four-dimensional spacetime current-density function of the free electron that propagates along the z-axis with velocity given by Eq. (84) corresponding to $r = r_0 = \rho_0$ is given 23 by substitution of Eq. (84) into Eq. (88).

$$J(\rho,\phi,z,t) = \left[\pi\left(\frac{\rho}{2\rho_0}\right) \frac{e}{\frac{4}{3}\pi\rho_0^3} \frac{\hbar}{m_e\sqrt{\rho_0^2 - \rho^2}} i_{\phi}\right] + \frac{e\hbar}{m_e\rho_0} \delta\left(z - \frac{\hbar}{m_e\rho_0}t\right) i_{\phi}. \tag{91}$$

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Table 1

The calculated electric (per electron), magnetic (per electron), and ionization energies for some two-electron atoms

Atom	/1 (a ₀)*	Electric energy ^b (eV)	Magnetic energy ^e (eV)	Calculated ionization energy ⁴ (eV)	Experimental ionization [12,13] energy (eV)
He	0.567	-23.96	0.63	24,59	24.59
Li ⁺	0.356	-76.41	2.54	75.56	75.64
Be ²⁺	0.261	-156.08	6.42	154.48	153.89
B³+	0.207	-262.94	12.96	260.35	259.37
C4+	0.171	-396.98	22.83	393.18	392.08
N5+	0.146	-558.20	36.74	552.95	552.06
O6+	0.127	-746.59	55.35	739.67	739.32
F ⁷⁺	0.113	-962.17	79.37	953.35	953.89

^{*}From Eq. (96).

1 The spacetime Fourier Transform is

$$\frac{e}{\frac{4}{3}\pi\rho_0^3}\frac{\hbar}{m_0}\operatorname{sinc}(2\pi s\rho_0) + 2\pi e\frac{\hbar}{m_0\rho_0}\delta(\omega - \mathbf{k}_e \bullet \mathbf{v}_z). \tag{92}$$

Spacetime harmonics of $\omega_n/c = k$ or $(\omega_n/c)\sqrt{\ell/\ell_0} = k$ do not exist. Radiation due to charge motion does not occur in any medium when this boundary condition is met. Thus, no

- 5 Fourier components that are synchronous with light velocity with the propagation constant $|\mathbf{k}_{\epsilon}| = \omega/c$ exist. Radiation
- 7 due to charge motion does not occur when this boundary condition is met. It follows from Eq. (84) and the relation-
- ship $2\pi\rho_0 = \lambda_0$ that the wavelength of the free electron is the de Broglie wavelength.

$$\lambda_0 = \frac{h}{m_0 v_0} = 2\pi \rho_0.$$

In the presence of a z-axis applied magnetic held, free electron precesses. The time average vector projection

of the total angular momentum of the respective on onto an axis S that rotates about the z-axis and z \(\), \(\), and the

- time averaged projection of the aguin communium onto the axis of the applied magnetic flet is ±70. Magnetic flux is
 linked by the electron in unable to a gnetic flux quantum
- with conservation of angular momentum as in the case of
- 19 the orbitsphere as the moneton of the angular momentum along the magnetic field is of h/2 reverses direction. The
- 21 energy, ΔE_{max} of the spin dip transition corresponding to the $m_s = \frac{1}{2}$ quantum number is given by Eq. (22).

$$\Delta E_{\text{max}}^{\text{spin}} = g\mu_{\text{B}} B_{\text{B}} + 4. \tag{94}$$

23 The Stern-Gerlach experiment implies a magnetic moment of one Bohr magneton and an associated angular momentum

25 quantum number of 1/2. Historically, this quantum number is called the spin quantum number, m_1 , and that designation

27 is maintained.

19. Two electron atoms

Two electron atoms may be solved from a central force balance equation with the pomentation condition. The force balance equation is

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$$\frac{m_0}{4\pi r_2^2} \frac{v_2^2}{r_2} = \frac{(s-7-1)^2 r_1^2}{4\pi c_1^2} + \frac{1}{4\pi r_2^2} \frac{\hbar^2}{Zm_0 r_2^2} \sqrt{s(s+1)}$$
 (95)

which gives the silius of both electrons as

$$r_1 = r_2 + \left(\frac{1}{Z-1} - \frac{\sqrt{s(s+1)}}{Z(Z-1)}\right), \quad s = \frac{1}{2}.$$
 (96)

19.1. Ionization energies calculated using the Poynting power theorem

For helium, which has no electric field beyond r_1 35 ionization energy(He) = -E(electric) + E(magnetic).

(97)

where

$$E(\text{electric}) = -\frac{(Z-1)e^2}{8\pi\epsilon n},\tag{98}$$

$$E(\text{magnetic}) = \frac{2\pi\mu_0 e^2 \hbar^2}{m_0^2 r^2}.$$
 (99)

For
$$3 \leq Z$$

ionization energy = -electric energy

$$-\frac{1}{Z}$$
 magnetic energy. (100)

The energies of several two-electron atoms are given in Table 1.

^bFrom Eq. (98).

[°]From Eq. (99).

^dFrom Eqs. (97) and (100).

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20. Elastic electron scattering from helium atoms

The aperture distribution function, $a(\rho, \phi, z)$, for the elastic scattering of an incident electron plane wave represented by $\pi(z)$ by a helium atom represented by

$$\frac{2}{4\pi(0.567a_0)^2}[\delta(r-0.567a_0)] \tag{101}$$

5 is given by the convolution of the plane wave with the helium atom function:

$$a(\rho,\phi,z) = \pi(z) \otimes \frac{2}{4\pi(0.567a_0)^2} [\delta(r - 0.567a_0)]. \quad (102)$$

7 The aperture function is

$$a(\rho,\phi,z) = \frac{2}{4\pi(0.567a_0)^2}$$

$$\sqrt{(0.567a_0)^2 - z^2}\delta(r - \sqrt{(0.567a_0)^2 - z^2}).$$
(103)

20.1. Far field scattering (circular symmetry)

Applying Huygens' principle to a disturbance caused by the plane wave electron over the helium atom as an aperture
 gives the amplitude of the far field or Fraunhofer diffraction pattern F(s) as the Fourier Transform of the aperture distribution. The intensity I₁^{ed} is the square of the amplitude.

$$F(s) = \frac{2}{4\pi(0.567a_0)^2} 2\pi \int_0^\infty \int_{-\infty}^\infty \sqrt{(0.567a_0)^2 - z^2} \delta(\rho - \sqrt{(0.567a_0)^2 - z^2})$$

$$\times J_0(s\rho) e^{-in\varepsilon} \rho \, \mathrm{d}\rho \, \mathrm{d}z, \tag{104}$$

$$I_1^{cd} = F(s)^2 =$$

$$I_{4} \left\{ \left[\frac{2\pi}{(z_{0}w)^{2} + (z_{0}s)^{2}} \right]^{1/2} \right. \\ \left\{ 2 \left[\frac{z_{0}s}{(z_{0}w)^{2} + (z_{0}s)^{2}} \right] J_{3/2} [((z_{0}w) + (z_{0}s)^{2})^{1/2}] \right\} \\ \left. - \left[\frac{z_{0}s}{(z_{0}w)^{2} + (z_{0}s)^{2}} \right]_{c}^{2} J_{3/2} [(z_{0}w) + (z_{0}s)^{2})^{1/2}] \right\}$$

$$(105)$$

$$s = \frac{4\pi}{1} \sin \frac{\theta}{2}$$
, we 0.0 m of A⁻¹). (106)

The experimental cost of Bromberg [15], the extrapolated experimental data of Hughes [15], the small angle data of Geiger [16] attiated semiexperimental results of Lassettre [15] for the elastic differential cross-section for the elastic scattering of electrons by helium atoms is shown graphically in Fig. 11. The elastic differential cross-section as a function of angle numerically calculated by Khare [15] using the first

21 Born approximation and first-order exchange approximation also appear in Fig. 11. These results which are based on a

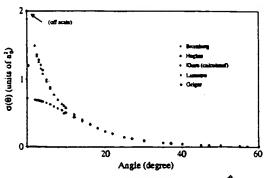


Fig. 11. The experimental results for the elastic differential cross-section for the elastic scattering of electrons by a firm atoms and a Born approximation prediction.

quantum mechanical model are comparative experimentation [15,16]. The closed form function Eqs. (105) and (106)) for the elastic differents cross action for the elastic scattering of electrons to help atoms is shown graphically in Fig. 12. The satisfies amplitude function, F(s) (Eq. (104), is shown as a insert. It is apparent from Fig. 11 that the quantum mechanical calculations fail completely at predicting the experimental results at small scattering angles; whereas, there is good agreement between Eq. (105) and the experimental results.

The fature of the chemical bond of hydrogen

The hydrogen molecule charge and current-density inctions, bond distance and energies are solved from the aplacian in ellipsoidal coordinates with the constraint of normaliation.

$$(\eta - \zeta)R_{\xi}\frac{\partial}{\partial \xi}\left(R_{\xi}\frac{\partial \phi}{\partial \xi}\right) + (\zeta - \xi)R_{\eta}\frac{\partial}{\partial \eta}\left(R_{\eta}\frac{\partial \phi}{\partial \eta}\right) + (\xi - \eta)R_{\xi}\frac{\partial}{\partial \zeta}\left(R_{\xi}\frac{\partial \phi}{\partial \zeta}\right) = 0.$$
 (107)

The force balance equation for the hydrogen molecule is

$$\frac{\hbar^2}{m_1 a^2 h^2} 2ab^2 X = \frac{e^2}{4\pi p_0} X + \frac{\hbar^2}{2m_1 a^2 b^2} 2ab^2 X,$$
 (108)

where 39

$$X = \frac{1}{\sqrt{\xi + a^2}} \frac{1}{\sqrt{\xi + b^2}} \frac{1}{c} \sqrt{\frac{\xi^2 - 1}{\xi^2 - \eta^2}}.$$
 (109)

Eq. (108) has the parametric solution

$$r(t) = ia\cos\omega t + jb\sin\omega t \tag{110}$$

when the semimajor axis, a, is

$$a = a_{\theta}. \tag{111}$$

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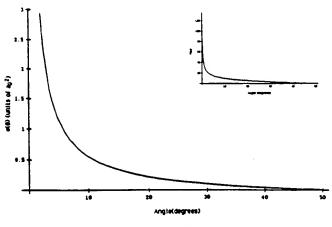


Fig. 12. The closed form function (Eqs. (105) and (106)) for the elastic differential cross section for the elastic scattering of electrons by helium atoms. The scattering amplitude function, F(s) (Eq. (104), is shown as an insert.

1 The internuclear distance, 2c', which is the distance between the foci is

$$2c' = \sqrt{2}a_{\bullet}. \tag{112}$$

3 The experimental internuclear distance is $\sqrt{2}a_0$. The semiminor axis is

$$b = \frac{1}{\sqrt{2}}a_0. {(113)}$$

5 The eccentricity, e, is

$$e=\frac{1}{\sqrt{2}}.$$

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21.1. The energies of the hydrogen molecule

7 The potential energy of the two electrons at the field of the protons at the foci is

$$V_{\bullet} = \frac{-2e^2}{8\pi\epsilon_0 \sqrt{a^2 - b^2}} \ln \frac{a + \sqrt{a^2 - b^2}}{a - \sqrt{a^2}} = 17.816 \text{ eV}.$$
(115)

9 The potential energy of the two press is

$$V_p = \frac{e^2}{8\pi \pi \sqrt{d^2 - M^2}} \tag{116}$$

The kinetic energy the electrons is

$$T = \frac{1}{2m_e a \sqrt{a^2 - b^2}} = 33.906 \text{ eV}. \quad (117)$$

11 The energy, V_m , of the magnetic force between the electrons is

$$V_{\rm m} = \frac{-\hbar^2}{4m_{\rm e}a\sqrt{a^2 - b^2}} \ln \frac{a + \sqrt{a^2 - b^2}}{a - \sqrt{a^2 - b^2}} = -16.9533 \text{ eV}.$$
(118)

The total energy is

$$E_{T} = V_{0} + T + V_{D} + V_{D}$$
 (119)

$$E_{\rm T} = -13.6 \,\mathrm{eV} \left[\left(2\sqrt{2} + \sqrt{2} + \frac{\sqrt{2}}{2} \right) \ln \frac{\sqrt{2} + 1}{\sqrt{2} - 1} - \sqrt{2} \right]$$

The exercise of two hydrogen atoms is

$$2H[a]_{\rm e} = -27.21 \text{ eV}.$$
 (121)

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The and dissociation energy, E_D , is the difference between the total energy of the corresponding hydrogen atoms e.g. (121) and E_T (Eq. (120)).

$$E_{\rm D} = E(2H[a_{\rm H}]) - E_{\rm T} = 4.43 \text{ eV}.$$
 (122)

The experimental energy determined by calorimetry is $E_D = 4.45 \text{ eV}$. (123)

22. Cosmological theory based on Maxwell's equations

Maxwell's equations and special relativity are based on the law of propagation of a electromagnetic wave front in the form

$$\frac{1}{c^2} \left(\frac{\partial \omega}{\partial t} \right)^2 - \left[\left(\frac{\partial \omega}{\partial x} \right)^2 + \left(\frac{\partial \omega}{\partial y} \right)^2 + \left(\frac{\partial \omega}{\partial z} \right)^2 \right] = 0. \quad (124)$$

For any kind of wave advancing with limiting velocity and capable of transmitting signals, the equation of front propagation is the same as the equation for the front of a light wave. Thus, the equation

$$\frac{1}{c^2} \left(\frac{\partial \omega}{\partial t} \right)^2 - (\operatorname{grad} \omega)^2 = 0 \tag{125}$$

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acquires a general character, it is more general than
Maxwell's equations from which Maxwell originally
derived it.

A discovery of the present work is that the classical wave

equation governs: (1) the motion of bound electrons, (2) the propagation of any form of energy, (3) measurements between inertial frames of reference such as time, mass, momentum, and length (Minkowski tensor), (4) fundamental particle production and the conversion of matter to energy, (5) a relativistic correction of spacetime due to particle production or annihilation (Schwarzschild metric), (6) the expansion and contraction of the universe, (7) the basis of the relationship between Maxwell's equations, Planck's equation, the de Broglie equation, Newton's laws, and special, and general relativity.

The relationship between the time interval between ticks t of a clock in motion with velocity v relative to an observer and the time interval t_0 between ticks on a clock at rest relative to an observer is [17]

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$$(ct)^{2} = (ct_{0})^{2} + (vt)^{2}. (126)$$

Thus, the time dilation relationship based on the constant maximum speed of light c in any inertial frame is

$$t = \frac{t_0}{\sqrt{1 - v^2/c^2}}. (127)$$

The metric $g_{\mu\nu}$ for Euclidean space is the Minkowski tensor $\eta_{\mu\nu}$. In this case, the separation of proper time between two events x^{μ} and $x^{\mu} + dx^{\mu}$ is $d\tau^2 = -\eta_{\mu\nu} dx^{\mu} dx^{\nu}$.

23. The equivalence of the gravitational mass and the inertial mass

- The equivalence of the gravitational mass and that tial mass, m_e/m_i = universal constant, which is
- 29 Newton's law of mechanics and gravitation set tally confirmed to less 1 x 10⁻¹¹ [18]. In plants, and discovered to less 1 x 10⁻¹¹ [18].
- 31 ery of a universal constant often leads the the elopment of an entirely new theory. From the universal constancy of the
- velocity of light, c the special theory of restrivity was derived; and from Planck's constant, the santum theory was
- deduced. Therefore, the universal constant m_g/m_i should be the key to the gravitation problem. The energy equation
 of Newtonian gravitation.

$$E = \frac{1}{2}mv^2 - \frac{GMm}{r_0} = \text{constant.}$$
 (128)

Since h, the angular momentum per unit mass, is

$$h = L/m = |\mathbf{r} \times \mathbf{v}| = r_0 v_0 \sin \phi$$

39 the eccentricity e may be written as

$$e = \left[1 + \left(v_0^2 - \frac{2GM}{r_0}\right) \frac{r_0^2 v_0^2 \sin^2 \phi}{G^2 M^2}\right]^{1/2},$$
 (129)

where m is the inertial mass of a particle, v_0 is the speed of the particle, r_0 is the distance of the particle from a massive object, ϕ is the angle between the direction of motion of the particle and the radius vector from the object, and M is the total mass of the object (including a particle). The eccentricity e given by Newton's differential equations of motion in the case of the central field permits the classification of the orbits according to the total energy E [19] (column 1) and the orbital velocity squared, v_0^2 , relative to the gravitational velocity squared, $2GM/r_0$ [19] (column 2):

$$E < 0$$
 $v_0^2 < \frac{2GM}{r_0}$ $e < 1$ ellipse,
 $E < 0$ $v_0^2 < \frac{2GM}{r_0}$ $e = 0$ circle (special case of ellipse),
 $E = 0$ $v_0^2 = \frac{2GM}{r_0}$ $e = 1$ parabolic orbit,
 $E > 0$ $v_0^2 > \frac{2GM}{r_0}$ $e > 1$ hyperbolic orbit. (130)

24. Continuity conditions for the production of a particle from a photon tracking in high speed

A photon traveline at the speed of light gives rise to a particle with an initial rank equal to its Compton wavelength

$$r = -\lambda_{\mathbf{C}} = \frac{1}{2\pi} r_{\mathbf{c}}^{*}. \tag{131}$$

The fartiste must have an orbital velocity equal to Newtoniah presentational escape velocity v_1 of the antiparticle.

$$v_0 = \sqrt{\frac{2Gm_0}{r}} = \sqrt{\frac{2Gm_0}{-\lambda_C}}.$$
 (132)

The eccentricity is one. The orbital energy is zero. The parmicle production trajectory is a parabola relative to the center of mass of the antiparticle.

The particle with a finite gravitational mass gives rise to a gravitational field that travels out as a front equivalent to a light wave front. The form of the outgoing gravitational field front traveling at the speed of light is f(t - r/c), and

$$dt^2 = f(r) dt^2 - \frac{1}{c^2} [f(r)^{-1} dr^2 + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2].$$
(133)

The speed of light as a constant maximum as well as phase matching and continuity conditions of the electromagnetic and gravitational waves require the following form of the squared displacements:

$$(c\tau)^2 + (v_{\mathbf{g}}t)^2 = (ct)^2, \tag{134}$$

$$f(r) = \left(1 - \left(\frac{v_{\rm g}}{c}\right)^2\right). \tag{135}$$

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In order that the wave front velocity does not exceed c in any frame, spacetime must undergo time dilation and length contraction due to the particle production event. The derivation and result of spacetime time dilation is analogous to the derivation and result of special relativistic time dilation wherein the relative velocity of two inertial frames replaces

the gravitational velocity.

The general form of the metric due to the relativistic effect

$$d\tau^{2} = \left(1 - \left(\frac{v_{g}}{c}\right)^{2}\right)dr^{2} - \frac{1}{c^{2}}\left[\left(1 - \left(\frac{v_{g}}{c}\right)^{2}\right)^{-1}dr^{2} + r^{2}d\theta^{2} + r^{2}\sin^{2}\theta\,d\phi^{2}\right]. \tag{136}$$

on spacetime due to mass m_0 with v_0 given by Eq. (132) is

The gravitational radius, r_s , of each orbitsphere of the particle production event, each of mass m_0 , and the corresponding general form of the metric are respectively

$$r_{\xi} = \frac{2Um}{c^{2}},$$

$$d\tau^{2} = \left(1 - \frac{r_{\xi}}{r}\right)dr^{2} - \frac{1}{c^{2}}\left[\left(1 - \frac{r_{\xi}}{r}\right)^{-1}dr^{2} + r^{2}d\theta^{2} + r^{2}\sin^{2}\theta\,d\phi^{2}\right].$$
(138)

13 The metric g_{pr} for non-Euclidean space due to the relativistic effect on spacetime due to mass m₀ is

$$g_{\mu\nu} = \begin{pmatrix} -(1 - \frac{2G_{ma}}{c^2 r^2}) & 0 & 0 & 0\\ 0 & \frac{1}{c^2} (1 - \frac{2G_{ma}}{c^2 r^2})^{-1} & 0 & 0\\ 0 & 0 & \frac{1}{c^2} r^2 & 0\\ 0 & 0 & 0 & \frac{1}{c^2} r^2 \sin^2 \theta \end{pmatrix}$$

15 Masses and their effects on spacetime superimpose The separation of proper time between two events x* and 17 is

$$d\tau^{2} = \left(1 - \frac{2GM}{c^{2}r}\right)dr^{2} - \frac{1}{c^{2}}\left[\left(1 - \frac{2GM}{c^{2}r}\right) + r^{2}d\theta^{2} + r^{2}\sin^{2}\theta d\phi^{2}\right]. \tag{140}$$

The Schwarzschild metrics (24 (149)) gives the relationship whereby matters auses relativistic corrections to spacetime that determine the covature of spacetime and 21 is the origin of gravity.

24.2. Particle production continuity conditions from Maxwell's equations, and the Schwarzschild metric

The photon to particle event requires a transition state
that is continuous wherein the velocity of a transition state
orbitsphere is the speed of light. The radius, r, is the Compton wavelength bar, $-\lambda_c$, given by Eq. (131). At production, the Planck equation energy, the electric potential energy, and the magnetic energy are equal to m_0c^2 .

The Schwarzschild metric gives the relationship whereby matter causes relativistic corrections to spacetime that determines the masses of fundamental particles. Substitution of $r = -\lambda_c$; dr = 0; $d\theta = 0$; $\sin^2\theta = 1$ into the Schwarzschild metric gives

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$$d\tau = dt \left(1 - \frac{2Gm_0}{c^2 r_e^2} - \frac{\sigma^2}{c^2} \right)^{1/2}$$
 (141)

with $v^2 = c^2$, the relationship between the proper time and the coordinate time is

$$\tau = ti\sqrt{\frac{2GM}{c^2r_e^a}} = ti\sqrt{\frac{2GM}{c^2 - \lambda_c}} = ti\frac{v_g}{c}.$$
 (142)

When the orbitsphere velocity is the specific light, continuity conditions based on the constant plantinum speed of light given by Maxwell's educations are mass energy = Planck equation energy = relative potential energy = magnetic energy = mass spacetime metric energy. Therefore,

$$m_0c^2 = \hbar\omega^* = V = E_{max} = \frac{1}{4\pi\epsilon_0 - \lambda_C} = \alpha^{-1} \frac{\pi\mu_0e^2\hbar^2}{(2\pi m_0)^2 - \lambda_C^3}$$

$$m_0c^2 = \hbar\omega^* = \frac{\hbar^{3/2}}{m_0 - \lambda_C^2} = \alpha^{-1} \frac{\pi\mu_0e^2\hbar^2}{(2\pi m_0)^2 - \lambda_C^3}$$

$$= \frac{\alpha^{3/2}}{1 \text{ sec}} \frac{-2c^2}{6m}.$$
(144)

The communications based on the constant maximum 43

The computer conditions based on the constant maximum speed of hight given by the Schwarzschild metric are:

$$\frac{\text{proper time}}{\text{coordinate time}} = i \frac{\sqrt{2Gm/c^2 - \lambda_C}}{\alpha} = i \frac{v_g}{\alpha c}.$$
 (145)

25. Masses of fundamental particles

Each of the Planck equation energy, electric energy, 47 and magnetic energy corresponds to a particle given by the relationship between the proper time and the coordi-49 nate time. The electron and down-down-up neutron correspond to the Planck equation energy. The muon and strange-strange-charmed neutron correspond to the electric 51 energy. The tau and bottom-bottom-top neutron correspond to the magnetic energy. The particle must possess the 53 escape velocity $v_{\mathbf{z}}$ relative to the antiparticle where $v_{\mathbf{z}} < c$. 55 According to Newton's law of gravitation, the eccentricity is one and the particle production trajectory is a parabola 57 relative to the center of mass of the antiparticle.

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1 25.1. The electron-antielectron lepton pair

A clock is defined in terms of a self-consistent system of units used to measure the particle mass. ² The proper time of the particle is equated with the coordinate time according to the Schwarzschild metric corresponding to light speed. The special relativistic condition corresponding to the Planck energy gives the mass of the electron.

$$2\pi \frac{\hbar}{mc^2} = \sec\sqrt{\frac{2Gm^2}{c\alpha^2\hbar}},\tag{146}$$

$$m_4 = \left(\frac{h\alpha}{\sec c^2}\right)^{1/2} \left(\frac{c\hbar}{2g}\right)^{1/4} = 9.1097 \times 10^{-31} \text{ kg.}$$
 (147)

$$m_e = 9.1097 \times 10^{-31} \text{ kg} - 18 \text{ eV}(\nu_e) = 9.1094 \times 10^{-31} \text{ kg},$$
(148)

$$m_{\rm e} = 9.1095 \times 10^{-31} \text{ kg.}$$
 (149)

25.2. Down-down-up neutron (DDU)

The corresponding equation for production of the neutron is

$$2\pi \frac{2\pi\hbar}{(m_N/3)[1/2\pi - \alpha/2\pi]c^2}$$

$$= \sec\sqrt{\frac{2G[(m_N/3)[1/2\pi - \alpha/2\pi]]^2}{3c(2\pi)^2\hbar}}, \qquad (150)$$

$$m_{N_{\text{calculated}}} = (3)(2\pi)\left(\frac{1}{1-\alpha}\right)\left(\frac{2\pi\hbar}{\sec c^2}\right)^{1/2}\left(\frac{2\pi(3)c\hbar}{2G}\right)^{1/4}$$

$$= 1.6744 \times 10^{-27} \text{ kg.} \qquad (151)$$

 $m_{\text{Nexperimental}} = 1.6749 \times 10^{-27} \text{ kg.}$

26. Gravitational potential energy

The gravitational radius, α_0 or r_0 , α_0 or is defined as

$$\alpha_0 = r_0 = \frac{Gm_0}{c^2}.$$
 (153)

² Presently the second a defined as the time required for 9,192,631,770 vibration where the cesium-133 atom. The "sec" as defined in Eq. (1901 is a fundamental constant, namely, the metric of spacetimetrit is almost identically equal to the present value for reasons explained in terf. [1]). A unified theory can only provide the relationships Between all measurable observables in terms of a clock defined in terms of fundamental constants according to those observables and used to measure them. The so defined "clock" measures "clicks" on an observable in one aspect, and in another, it is the ruler of spacetime of the universe with the implicit dependence of spacetime on matter—energy conversion as shown in the Relationship of Matter to Energy and Spacetime Expansion section.

When $r_0 = r_0^* = -\lambda_C$, the gravitational potential energy equals $m_0 c^2$

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$$r_{\rm G} = \frac{Gm_0}{c^2} = -\lambda_{\rm C} = \frac{\hbar}{m_0c},\tag{154}$$

$$E_{\text{grev}} = \frac{Gm_0^2}{r} = \frac{Gm_0^2}{-\lambda_C} = \frac{Gm_0^2}{r_0^2} = \hbar\omega^* = m_0c^2.$$
 (155)

The mass m_0 is the Planck mass, m_v ,

$$m_{\rm u} = m_0 = \sqrt{\frac{\hbar c}{G}}.$$
 (156)

The corresponding gravitational velocity, v_0 , is defined as

$$v_{\rm O} = \sqrt{\frac{Gm_0}{r}} = \sqrt{\frac{Gm_0}{-\lambda_{\rm C}}} = \sqrt{\frac{Gm_u}{-\lambda_{\rm C}}}.$$

26.1. Relationship of the equivalence of particle production energies

For the Planck mass parties, it a relationships corresponding to Eq. (144) are: (mass except) = Planck equation energy = electric potential energy = mass/spacetime metric energy)

$$m_0 c^2 = \hbar \omega^* + E_{\text{mag}} = E_{\text{grav}} = E_{\text{spacetime}}$$
 (158)

$$c_{c}^{2} = h_{c}^{2} = \frac{1}{m_{0} - \lambda_{c}^{2}} = a^{-1} \frac{e^{2}}{4\pi\epsilon_{0} - \lambda_{c}} = a^{-1} \frac{\pi\mu_{0}e^{2}h^{2}}{(2\pi m_{0})^{2} - \lambda_{c}^{2}}$$

$$= a^{-1} \frac{\mu_{0}e^{2}c^{2}}{2h} \sqrt{\frac{Gm_{0}}{-k_{c}}} \sqrt{\frac{\hbar c}{G}} = \frac{ah}{1 \sec \sqrt{\frac{-\lambda_{c}c^{2}}{2Gm}}}. \quad (159)$$

hese equivalent energies give the particle masses in terms of the gravitational velocity, vo and the Planck mass, m.

$$m_{0} = \alpha^{-1} \frac{\mu_{0}e^{2}c}{2h} \frac{\sqrt{Gm_{0}/-\lambda_{C}}}{c} m_{e} = \alpha^{-1} \frac{\mu_{0}e^{2}c}{2h} \sqrt{\frac{Gm_{0}}{c^{2}-\lambda_{C}}} m_{e}$$

$$= \alpha^{-1} \frac{\mu_{0}e^{2}c}{2h} \frac{v_{0}}{c} m_{e} = \frac{v_{0}}{c} m_{e}. \tag{160}$$

26.2. Planck mass particles

A pair of particles each of the Planck mass corresponding to the gravitational potential energy is not observed since the velocity of each transition state orbitsphere is the gravitational velocity v_0 that in this case is the speed of light, whereas, the Newtonian gravitational escape velocity v_0 is $\sqrt{2}$ the speed of light. In this case, an electromagnetic wave of mass energy equivalent to the Planck mass travels in a circular orbit about the center of mass of another electromagnetic wave of mass energy equivalent to the Planck mass wherein the eccentricity is equal to zero and the escape velocity can never be reached. The Planck mass is a measuring stick. The extraordinarily high Planck mass

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 $(\sqrt{\hbar c/G} = 2.18 \times 10^{-8} \text{ kg})$ is the unobtainable mass bound imposed by the angular momentum and speed of the photon relative to the gravitational constant. It is analogous to the unattainable bound of the speed of light for a particle possessing finite rest mass imposed by the Minkowski tensor.

26.3. Astrophysical implications of Planck mass particles

7 The limiting speed of light eliminates the singularity problem of Einstein's equation that arises as the radius of a blackhole equals the Schwarzschild radius. General relativity with the singularity eliminated resolves the paradox of the infinite propagation velocity required for the gravitational force in order to explain why the angular momentum of objects 13 orbiting a gravitating body does not increase due to the finite propagation delay of the gravitational force according to spe-15 cial relativity [20]. When the gravitational potential energy density of a massive body such as a blackhole equals that of a particle having the Planck mass, the matter may transition to photons of the Planck mass. Even light from a blackhole will escape when the decay rate of the trapped matter with the concomitant spacetime expansion is greater than the effects of gravity which oppose this expansion. Gamma-ray bursts are the most energetic phenomenon known that can release an explosion of gamma rays packing 100 times more energy than a supernova explosion [21]. The annihilation of a blackhole may be the source of gamma-ray bursts. The source may be due to conversion of matter to photons of the Planck mass/energy which may also give rise to cosmic rays which are the most energetic particles known, and their origin is also a mystery [22]. According to the GZK cutoff, the cosmic spectrum cannot extend beyond 5×10^{19} eV, but AGASA, the world's largest air shower array, has shown that 31 the spectrum is extending beyond 1020 eV without any elean sign of cutoff [23]. Photons each of the Planck mass day the the source of these inexplicably energetic cosmic rays

27. Relationship of matter to energy and spacetime expansion

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The Schwarzschild metric gives the relationship whereby 37 matter causes relativistic corrections to decetime. The limiting velocity c results in the contraction of spacetime due to particle production, which is given by $2\pi r_{\rm g}$ where $r_{\rm g}$ is the gravitational radition of the particle. This has implications for the expansion to the expansion of the expansion energy. Q the massagergy to expansion/contraction quotient of spacetime is given by the ratio of the mass of a particle at production divided by T, the period of production.

$$Q = \frac{m_0}{T} = \frac{m_0}{\frac{2\pi r_0}{c}} = \frac{m_0}{\frac{2\pi \frac{10m_0}{c^2}}{c}} = \frac{c^3}{4\pi G} = 3.22 \times 10^{34} \text{ kg/sec.}$$
(161)

The gravitational equations with the equivalence of the particle production energies (Eq. (144)) permit the conservation of mass/energy ($E = mc^2$) and spacetime ($c^3/4\pi G = 3.22 \times$ 10^{34} kg/sec). With the conversion of 3.22×10^{34} kg of matter to energy, spacetime expands by I sec. The photon has inertial mass and angular momentum, but due to Maxwell's equations and the implicit special relativity it does not have a gravitational mass.

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27.1. Cosmological consequences

The universe is closed (it is finite but with no boundary). It is a 3-sphere universe-Riemannian three-dimensional hyperspace plus time of constant positive curvature at each r-sphere. The universe is oscillatory in matter/energy and spacetime with a finite minimum radius, the gravitational radius. Spacetime expands as mass is released as energy which provides the basis of the atomic, the state and and cosmological arrows of time. Different resons of space are isothermal even though they are senarated by scatter distances than that over which light could have during the time of the expansion of the universe [24] Presently, stars and large-scale structures of the present apparation as stellar, galaxy, and supercluster evolution occurred during the contraction phase [25-31]. The maximum power radiated by the universe which occurs at the beginning of the expansion phase is $P_U = c^5/4469 \times 10^{51}$ W. Observations beyond the beginning of the extransion phase are not possible since the was entirely matter filled. univend

riod of oscillation of the universe based on d propagation of light

Mass/energy is conserved during harmonic expansion and **Intraction.** The gravitational potential energy E_{max} given by Eq. (155) with $m_0 = m_U$ is equal to $m_U c^2$ when the radius of the universe r is the gravitational radius r_0 . The gravitational velocity v_0 (Eq. (157) with $r = r_0$ and $m_0 = m_0$) is the speed of light in a circular orbit wherein the eccentricity is equal to zero and the escape velocity from the universe can never be reached. The period of the oscillation of the universe and the period for light to transverse the universe corresponding to the gravitational radius ro must be equal. The harmonic oscillation period, T, is

$$T = \frac{2\pi r_0}{c} = \frac{2\pi G m_0}{c^3} = \frac{2\pi G (2 \times 10^{54} \text{ kg})}{c^3}$$
$$= 3.10 \times 10^{19} \text{ sec} = 9.83 \times 10^{11} \text{ years,}$$
(162)

where the mass of the universe, m_U , is approximately 2 × 10^{54} kg. (The initial mass of the universe of 2×10^{54} kg is based on internal consistency with the size, age, Hubble constant, temperature, density of matter, and power spectrum.) Thus, the observed universe will expand as mass is released as photons for 4.92×10^{11} years. At this point in its world line, the universe will obtain its maximum size and begin to contract.

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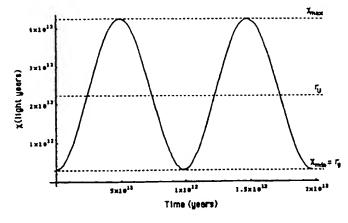


Fig. 13. The radius of the universe as a function of time.

28. The differential equation of the radius of the universe

Based on conservation of mass/energy $(E = mc^2)$ and spacetime $(c^3/4\pi G = 3.22 \times 10^{34} \text{ kg/sec})$. The universe behaves as a simple harmonic oscillator having a restoring force, F, which is proportional to the radius. The proportionality constant, k, is given in terms of the potential energy, E, gained as the radius decreases from the maximum expansion to the minimum contraction.

$$\frac{E}{\aleph^2} = k \tag{163}$$

Since the gravitational potential energy E_{prev} is equal to muc² when the radius of the universe r is the gravitational radius;
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$$F = -k\aleph = -\frac{m_{\mathrm{U}}c^2}{r_{\mathrm{G}}^2}\aleph = -\frac{m_{\mathrm{U}}c^2}{(Gm_{\mathrm{U}}/c^2)^2}\aleph.$$

And, the differential equation of the radius of the radius

$$m_{\mathrm{U}} \aleph + \frac{m_{\mathrm{U}} c^2}{r_{\mathrm{U}}^2} \aleph = m_{\mathrm{U}} \aleph + \frac{m_{\mathrm{U}} c^2}{(G m_{\mathrm{U}})^2}$$
(165)

The maximum radius of the inverse the amplitude, ro.

15 of the time harmonic variable in transmus of the universe, is given by the quotient on the total mass of the universe and 17 Q (Eq. (161)), the mass contraction quotient.

$$r_0 = \frac{m_U}{Q} = \frac{1}{c^2/4\pi G}$$

$$= 1.97 \times 10^{24} \text{ fight years.}$$
(166)

The minimum radius which corresponds to the gravitational radius, r_0 , given by Eq. (137) with $m_0 = m_0$ is

$$r_{\rm g} = \frac{2Gm_{\rm U}}{c^2} = 2.96 \times 10^{27} \text{ m} = 3.12 \times 10^{11} \text{ light years.}$$
21 (167)

When the radius of the universe is the gravitational radius, $r_{\rm g}$, the proper time is equal to the conditional time by Eq. (142), and the gravitational escale we occup $v_{\rm g}$ of the universe is the speed of light. The radius of the universe as a function of time as shown in rights is

$$R = \begin{pmatrix} r_{\rm g} + \frac{cm_{\rm H}}{Q} \end{pmatrix} \frac{cm_{\rm H}}{Q} \cos\left(\frac{2\pi t}{(2\pi r_{\rm Q}/c)}\right)$$

$$= \frac{cm_{\rm H}}{(c^3/4\pi G)} + \frac{cm_{\rm H}}{(c^3/4\pi G)} - \frac{cm_{\rm H}}{(c^3/4\pi G)} \cos\left(\frac{2\pi t}{(2\pi Gm_{\rm H}/c^3)}\right). \tag{168}$$

The expansion/contraction rate, N, as shown in Fig. 14 is

$$\mathring{\aleph} = 4\pi c \times 10^{-3} \sin\left(\frac{2\pi t}{(2\pi G m_U/c^3)}\right) \text{ km/sec.}$$
 (169)

29. The Hubble constant

The Hubble constant is given by the ratio of the expansion rate given in units of km/sec divided by the radius of the expansion in Mpc. The radius of expansion is equivalent to the radius of the light sphere with an origin at the time point when the universe stopped contracting and started to expand.

$$H = \frac{\aleph^{\bullet}}{t \text{Mpc}} = \frac{4\pi c \times 10^{-3} \sin\left(\frac{2\pi t}{(2\pi Gm_0/c^2)}\right) \text{km/sec}}{t \text{Mpc}}.$$
 (170)

For $t = 10^{10}$ light years = 3.069×10^3 Mpc, the Hubble constant, H_0 , is

$$H_0 = 78.6 \text{ km/sec Mpc.}$$
 (171)

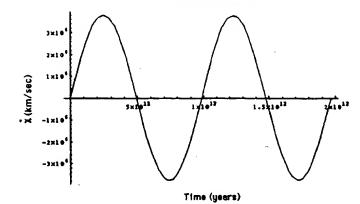


Fig. 14. The expansion/contraction rate of the universe as a function of time.

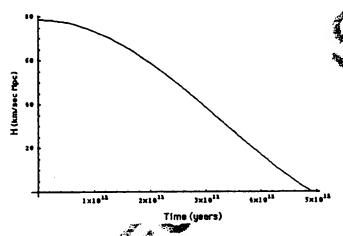


Fig. 15. The Hubble country of the universe as a function of time.

1 The experimental value [34] as shown in $H_0 = 80 \pm 17$ km/sec Mpc. (172)

30. The density of the universe a a function of time

The density of the universe at a function of time $\rho_U(t)$ given by the ratio of the property and function of time and the volume as a function as shown in Fig. 16 is

$$\rho_{U}(t) = \frac{m_{U}(t)}{p} = \frac{m_{U}(t)}{2} \left(1 + \cos\left(\frac{2\pi t}{2\pi G_{m_{U}}}\right)\right)$$

$$\frac{4}{3}\pi \left(\left(\frac{2G_{m_{U}}}{c^{2}} + \frac{G_{m_{U}}}{2}\right) - \frac{G_{m_{U}}}{2}\cos\left(\frac{2\pi t}{2\pi G_{m_{U}}}\right)\right)^{3}.$$
(173)

- For $t = 10^{10}$ light years, $\rho_{\rm U} = 1.7 \times 10^{-32}$ g/cm³. The density of luminous matter of stars and gas of galaxies is about $\rho_{\rm U} = 2 \times 10^{-31}$ g/cm³ [33,34].
- 31. The power of the universe as a function of time $P_U(t)$

From $E = mc^2$ and Eq. (161),

$$P_{\rm U}(t) = \frac{c^3}{8\pi G} \left(1 + \cos\left(\frac{2\pi t}{2\pi r_{\rm G}/c}\right) \right). \tag{174}$$

For $t = 10^{10}$ light years, $P_{\rm U}(t) = 2.88 \times 10^{51}$ W. The observed power is consistent with that predicted. The power of the universe as a function of time is shown in Fig. 17.

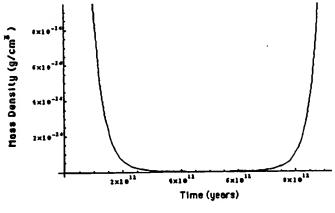


Fig. 16. The density of the universe as a function of time.

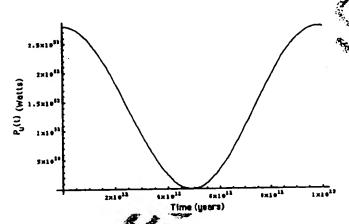


Fig. 17. The powers there hiverse as a function of time.

32. The temperature of the universe sale ion of time

The temperature of the universe as a function of time, $T_U(t)$, as shown in Fig. 18 How from the Stefan-Boltzmann law.

$$T_{U}(t) = \left(\frac{1}{1 + e^{\frac{2\pi i U(t)}{2\pi i V(t)}}}\right)^{1/4} = \left(\frac{1}{1 + \frac{G \log(t)}{c^{2} N(t)}}\right) \left[\frac{A_{U}(t)}{e \sigma}\right]^{1/4}.$$
 (175)

The calculated uniform temperature is about 2.7 K which is in agreement with the observed microwave background
 temperature [32].

33. Power spectrum of the cosmos

The power spectrum of the cosmos, as measured by the Las Campanas survey, generally follows the prediction of cold dark matter on the scales of 200-600 million light-years. However, the power increases dramatically on scales of 600-900 million light-years [31]. This discrepancy means that the universe is much more structured on those scales than current theories can explain.

The universe is oscillatory in matter/energy and spacetime with a finite minimum radius. The minimum radius which corresponds to the gravitational radius, $r_{\rm g}$, given by Eq. (167) is 3.12×10^{11} light years. The minimum radius is larger than that provided by the current expansion, approximately 10 billion light years [32]. The universe is a four-dimensional hyperspace of constant positive curvature at each r-sphere. The coordinates are spherical, and 9

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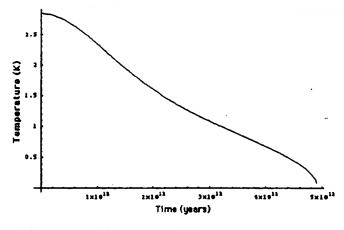


Fig. 18. The temperature of the universe as a function of time during the expansion phase

the space can be described as a series of spheres each of constant radius r whose centers coincide at the origin. The existence of the mass mu causes the area of the spheres to be less than 4πr² and causes the clock of each r-sphere to run so that it is no longer observed from other r-spheres to be at the same rate. The Schwarzschild metric given by Eq. (140) is the general form of the metric which allows for these effects. Consider the present observable universe that has undergone expansion for 10 billion years. The radius of the universe as a function of time from the coordinate r-sphere is of the same form as Eq. (168). The average size of the universe, ru, is given as the sum of the gravitational radius, rs, and the observed radius, 10 billion light years.

$$r_0 = r_g + 10^{10}$$
 light years = 3.12 × 10¹¹ light years
+10¹⁰ light years = 3.22 × 10¹¹ light years

The frequency of Eq. (168) is one-l 15 spacetime expansion from the conthe mass of universe into energy according to H Thus, keeping the same relationships, the frequ current expansion function is the reciprocal one-ba ir use current age. Substifunction is the average size 19 of the niverse, the frequency of expansion, and the amp expansion, 10 billion light the radius of the universe as a 21 years, into Eq. e coordinate r-sphere. function of tirk

$$R = 3.22 \times 10^{10} \times 10^{10}$$

$$\cos\left(\frac{2\pi t}{5 \times 10^9 \text{ light years}}\right) \text{ light years.}$$
 (177)

23 The Schwarzschild metric gives the relationship between the proper time and the coordinate time. The infinitesimal

temporal displacement, d_1^2 is given by Eq. (140). In the case that $dr^2 = d\theta^2 = d\phi^2$ the relationship between the proper time and the coordinate time is

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$$d\tau^2 = \left(1 - \frac{2Gm_V}{G^2}\right) dr^2, \tag{178}$$

The maximum power radiated by the universe is given by Figs. (174) which occurs when the proper radius, the co-dinate radius, and the gravitational radius r_8 are equal. For the present universe, the coordinate radius is given by Eq. (176). The gravitational radius is given by Eq. (167). The maximum of the power spectrum of a trigonometric function occurs at its frequency [35]. Thus, the coordinate maximum power according to Eq. (177) occurs at 5×10^9 light years. The maximum power corresponding to the proper time is given by the substitution of the coordinate radius, the gravitational radius r_8 , and the coordinate power maximum into Eq. (179). The power maximum in the proper frame occurs at

$$\tau = 5 \times 10^9 \text{ light years} \sqrt{1 - \frac{3.12 \times 10^{11} \text{ light years}}{3.22 \times 10^{11} \text{ light years}}},$$

$$\tau = 880 \times 10^6 \text{ light years}.$$
(180)

The power maximum of the current observable universe is predicted to occur on the scale of 880×10^6 light years. There is excellent agreement between the predicted value and the experimental value of $600-900 \times 10^6$ light years [31].

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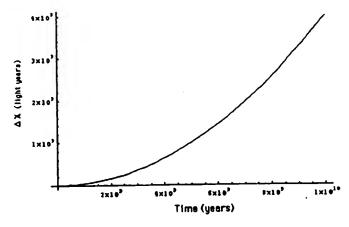


Fig. 19. The differential expansion of the light sphere due to the acceleration of the expansion of the cosmos as a

34. The expansion/contraction acceleration, ℵ

The expansion/contraction acceleration rate, R, as shown in Fig. 19, is given by the time derivative of Eq. (169).

$$\stackrel{\bullet \bullet}{\aleph} = 2\pi \frac{c^4}{Gm_U} \cos\left(\frac{2\pi t}{2\pi Gm_U/c^3} \sec\right) \stackrel{\bullet \bullet}{\aleph} = H_{\bullet}$$

$$= 78.7 \cos\left(\frac{2\pi t}{3.01 \times 10^5 \text{ Mpc}}\right) \text{km/sec Mpc.}$$
(181)

The differential in the radius of the universe, $\triangle \aleph$, due to its acceleration is given by $\triangle \aleph = 1/2\bar{\aleph}t^2$. The differential in expanded radius for the elapsed time of expansion, $t = 10^{10}$ light years corresponds to a decease in brightness of a supernovae standard candle of about an order of tage initude of that expected where the distance is takent $\triangle \aleph$. This result based on the predicted rate of acceleration and the expansion is consistent with the experiment observation [36-38].

Furthermore, the microwave background addition image obtained by the Boomerang telescope is consistent with a universe of nearly flat geometry flats, the commencement of its expansion. The data is consistent with a large offset radius of the universe with standard later case in size since the commencement of expansion about 10 billion years ago.

35. Power spectral or incomic microwave background

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When the waximum contribution of the amplitude, sponding to the maximum contribution of the amplitude, ro, of the time harmonic variation in the radius of the universe, (Eq. (166)), it is entirely radiation filled. Since the photon has no gravitational mass, the radiation is uniform. As energy converts into matter the power of the universe may be considered negative for the first quarter cycle start-

ing from the point of maximum expansion as given by Eq. (187), and spacetime contracts according to Eq. (161). The gravitational field from parties production travels as a light wave front. As the united contracts to a minimum radius, the gravitational radius even by Eq. (167), constructive interference of the gravitational fields occurs for distances which are integer of the amplitude, ro, of the time harmonic variation in the ractus of the universe for the times when the poster is negative according to Eq. (187). The resulting slightstandions in the density of matter are observed from present sphere. The observed radius of expansion is equivalent to the radius of the light sphere with an origin at the time point when the universe stopped contracting and sourced to expand. The spherical harmonic parameter & is ven by the ratio of the amplitude, ro, of the time harmonic variation in the radius of the universe, (Eq. (166)) divided by the present radius of the light sphere where the universe is a 3-sphere universo-Riemannian three-dimensional hyperspace plus time of constant positive curvature at each r-sphere. For $t = 10^{10}$ light years = 3.069 × 10³ Mpc, the fundamental & is given by

$$\ell = \frac{r_0}{t} = \frac{2 \times 10^{54} \text{ kgc}^3/4\pi G}{t}$$

$$= \frac{1.97 \times 10^{12} \text{ light years}}{10^{10} \text{ light years}} = 197.$$
(182)

The number of constructive interferences is given by the maximum integer of the ratio of the amplitude, ro, of the time harmonic variation in the radius of the universe, (Eq. (166)) divided by the minimum radius, the gravitational radius (Eq. (167)). The number of peaks are

$$\frac{r_0}{r_0} = \frac{\frac{2 \times 10^{34} \text{ kg}}{c^2 / 4 \pi G}}{2 Gm_0 / c^2} = \frac{1.97 \times 10^{12} \text{ light years}}{3.12 \times 10^{11} \text{ light years}} = 6.3 \rightarrow 6. (183)$$

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Table 2 Predicted harmonic parameters l and relative intensities l(n) as a function of peak n

п	•	$I(n)^b$
1	197	1
2	591	0.50
3	788	0.33
4	985	0.25
5	1182	0.20
6	1379	0.17

Eq. (184). ^bEq. (188).

The peaks are predicted to occur at the fundamental plus harmonics of the fundamental-integer multiples, n = 2, 3, 4, 5, and 6, of the fundamental $\ell = 197$. 3

$$l = 197$$
 (fundamental),
 $l = 197 + n197$ $n = 2, 3, 4, 5, and 6 (harmonics). (184)$

From Eq. (184), the predicted harmonic parameters & are given in Table 2.

The harmonic peaks correspond to the condition that the amplitude of the harmonic term of the radius of the universe $r_0(n)$ is a reciprocal integer that of the maximum amplitude r_0 . Thus, $r_0(n)$ is given by

$$r_0(n) = \frac{r_0}{n} = \frac{\frac{2 \times 10^{14} \text{ kg}}{c^2/4\pi G}}{n} = \frac{1.97 \times 10^{12} \text{ light years}}{n}.$$
 (185)

The power flow of radiant energy into mass decreases as the radius contracts, and the relative intensities of the 11 peaks follow from the power flow. The relative int are given by the normalized power as a function 13 the time at which the magnitude of the amp harmonic term of the radius of the universe Eq. (185) corresponding to each contrag constructive interference occurs. Star point of the maximum expension the universe is entirely radiation filled and the VB is mile in, the time at which the magnitude of the and ude of the harmonic term of the radius of the universe ro(1) given by Eq. (185) follows from Eq. (168).

$$r_0(n) = \frac{r_0}{n} = \frac{1.9^2}{4}$$

$$= 1.9^{12} \cdot 10^{12} \cos\left(\frac{2\pi t(n)}{9.83 \times 10^{11} \text{ years}}\right) \text{ light years,}$$

$$t(n) = \frac{9.83 \times 10^{11}}{2\pi} \cos^{-1}\left(\frac{1}{n}\right) \text{ years}$$

$$= 1.564 \times 10^{11} \cos^{-1}\left(\frac{1}{n}\right) \text{ years.}$$
 (186)

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The power of the universe as a function of time is given by Eq. (174) and is shown in Fig. 17. To express the negative power flow relative to the radiant energy of the universe corresponding to the conversion of energy into matter, the power of the universe as a function of time may be expressed

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$$P_{U}(t) = -\frac{c^{5}}{4\pi G} \cos\left(\frac{2\pi t}{9.83 \times 10^{11} \text{ years}}\right) W,$$

$$P_{U}(t) = -2.9 \times 10^{51} \cos\left(\frac{2\pi t}{9.83 \times 10^{11} \text{ years}}\right) W, \quad (187)$$

where t = 0 corresponds to the time when the universe reaches the maximum radius corresponding to the maximum contribution of the amplitude, ro, of the time harmonic variation in the radius of the universe (For 166)). At t = 0 as defined, the universe is entirely radiation filled, and the power into particle production is a maximum. At $t = (\pi/2)/(2\pi/9.83 \times 10^{11} \text{ years})$ particle production is in balance with matter to energy conversion, and the latter dominates for the following half

cycle.

The relative intensity given by substitution of Eq. (186) into Eq. (147) that is normalized by the magnitude of the maximum power which occurs at the maximum radius. Thus, the relative intensities are given by

$$I(n) = \cos\left(\frac{2\pi(1.334 \times 10^{11} \cos^{-1}(\frac{1}{n})\text{years})}{9.83 \times 10^{11} \text{ years}}\right) = \frac{1}{n}. (188)$$

The relative intensities I(n) as a function of peak n are given

in Table 2.

The cosmic microwave background radiation is an average temperature of 2.7 K, with deviations of 30 or so μK In different parts of the sky representing slight variations in the density of matter. The measurements of the anisotropy in the Cosmic Microwave Background (CMB) have been measured with the Degree Angular Scale Interferometer (DASI) [40]. The angular power spectrum was measured in the range 100 < l < 900, and peaks in the power spectrum from the temperature fluctuations of the cosmic microwave background radiation appear at certain values of & of spherical harmonics. Peaks were observed at $\ell \approx 200$, $\ell \approx 550$, and $\ell \approx 800$ with relative intensities of 1, 0.5, and 0.3, respectively (Fig. 1 of Ref. [40]). There is excellent agreement between the predicted parameters given in Table 2 and the observed peaks.

36. The periods of spacetime expansion/contraction and particle decay/production for the universe are equal

The period of the expansion/contraction cycle of the 63 radius of the universe, T, is given by Eq. (162). It follows from the Poynting power theorem with spherical radiation 65 that the transition lifetimes are given by the ratio of energy

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and the poveer of the transition (Eqs. (60)-(61)). Exponential decay applies to electromagnetic energy decay

$$h(t) = e^{-(1/T)t}u(t).$$
 (189)

- The coordinate time is imaginary because energy transitions are spacelike due spacetime expansion from matter to en-
- ergy conversion. For example, the mass of the electron (a fundamental particle) is given by

$$\frac{2\pi - \lambda_{\mathbf{C}}}{\sqrt{2Gm_{\mathbf{e}}/-\lambda_{\mathbf{C}}}} = \frac{2\pi - \lambda_{\mathbf{C}}}{v_{\mathbf{g}}} = i\alpha^{-1} \sec, \tag{190}$$

- where v_e is Newtonian gravitational velocity (Eq. (132)). When the gravitational radius r_1 is the radius of the universe,
- the proper time is equal to the coordinate time by Eq. (142), and the gravitational escape velocity v_g of the universe is
- the speed of light. Replacement of the coordinate time, t, by the spacelike time, it, gives

$$h(t) = Re[e^{-i(1/T)t}] = \cos\frac{2\pi}{T}t,$$
 (191)

- where the period is T (Eq. (162)). The continuity conditions based on the constant maximum speed of light
- (Maxwell's equations) are given by Eqs. (143)-(144). The 15 continuity conditions based on the constant maximum speed
- of light (Schwarzschild metric) are given by Eq. (145). The periods of spacetime expansion/contraction and par-
- ticle decay/production for the universe are equal because only the particles which satisfy Maxwell's equations and
- the relationship between proper time and coordinate time 21 imposed by the Schwarzschild metric may exist.

37. Wave equation

The general form of the light front wave equation is by Eq. (124). The equation of the radius of the university may be written as

$$R = \left(\frac{2Gm_U}{c^2} + \frac{cm_U}{(c^3/4\pi G)}\right) - \frac{cm_U}{c^3/4\pi G}\cos\left(\frac{2\pi}{(2\pi Gm_U/c^3)}\right) m, \quad (192)$$

amat h for a light wave which is a solution of the waye 27 front.

38. Conclusion Maxwell equations, Planck's equation, the de Broglie equation, Newton's laws, and special, and general relativity are unified.

39. Uncited References

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